

**University of Kentucky**  
**Department of Physics and Astronomy**  
**PHY 525: Solid State Physics II**  
**Fall 2000**  
**Test 2**

Date: November 8, 2000 (Wednesday)

Time allowed: 50 minutes.

Answer all questions.

1. **Hall coefficient of a semiconductor.** (a) Starting from drift velocity approximation, show that the Hall coefficient of a semiconductor is given by

$$R_H = \frac{1}{n_i e c} \frac{1-b}{1+b}$$

where  $n_i$  is the intrinsic concentration, and  $b$  is the ratio of mobility in conduction and valance bands ( $b = \mu_n / \mu_p$ ). (b) Consider two semiconductors A and B of with same energy gap. The following table gives the ratio of electron effective mass and relaxation time in the conduction and valance bands:

	$m_n^* / m_p^*$	$\tau_n / \tau_p$
Semiconductor A	0.3	30
Semiconductor B	0.8	15

Estimate the ratio of their Hall coefficients from Drude model. (c) For a semiconductor of energy gap equivalent to a temperature of 12500K, estimate the ratio of the Hall coefficient at 300K and 200K,  $R_H(300K) / R_H(200K)$ . Assume  $\tau$  does not vary much in this temperature range.

2. **Graded diode.** In the depletion layer (width  $2w$ ) of a graded p-n junction, the doping level varies linearly with position:  $N_D - N_A = kx$  for  $-w \leq x \leq +w$ . If the p- and n-semiconductors have doping level of  $N_A$  and  $N_D$  respectively. Let the effective density of state of the conduction and valance band be  $N_C$  and  $N_V$  respectively. Also let the energy gap of the intrinsic semiconductor be  $E_g$ . Assume all impurities are fully ionized. (a) Calculate chemical potential  $\mu_n$  and  $\mu_p$  in terms of  $N_D$ ,  $N_A$ ,  $N_C$ ,  $N_V$ , and  $E_g$ , from this calculate the potential difference  $\Delta\phi$  across the depletion layer. (b) What should be the electric field  $E$  at the two sides of the depletion layer? Find the electric field  $E(x)$  within the depletion layer. (c) Find the electric potential  $\phi(x)$  within the depletion layer. (d) Determine the layer width  $2w$  in term of  $\Delta\phi$ .