

**University of Kentucky**  
**Department of Physics and Astronomy**

PHY 525. Introduction to Solid State Physics II

Test 2.

Date: Oct 12, 2001

Time: 9:00-9:50

Answer all questions.

1. (25 points)

The electron energy near the top of the valance band in a semiconductor is given by

$$E_v = -10^{-37} k^2 \quad (E_v \text{ in Joules, } k \text{ in } m^{-1})$$

where  $\mathbf{k}$  is the wavevector. An electron is removed from the state

$$\mathbf{k} = 10^9 \hat{k}_x \quad m^{-1}$$

where  $\hat{k}_x$  is a unit vector along the x axis. Calculate the following quantities of the resulting hole:

- (i) The effective mass.
- (ii) The energy.
- (iii) The momentum.
- (iv) The velocity.

Each quantity must include the sign (or direction).

2. (25 points)

Consider the close orbits of an electron in real space and k space when an external magnetic field B is applied. Let the area be A and S respectively. Note that the magnet flux BA is quantized in unit of  $\Phi_0 = h/e$ .

- (i) Write down the relationship between A and S and hence the relationship between S and B.
- (ii) Calculate S for a metal X of valance 1 (i.e. one conducting electron per atom). The atomic density of the metal is  $8.5 \times 10^{28} m^{-3}$ . Assume free electron model.
- (iii) In a de Haas-van Alphen experiment of metal X, the magnetic susceptibility is oscillating periodically with  $\delta(1/B)$ . Calculate the periodicity. How many oscillations are there as B is changed from 10.70 T to 10.93T?