

PHYSICS OF ACTIVE GALACTIC NUCLEI

活動銀河核の物理学

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LECTURE 2:

SUPERMASSIVE BLACK HOLES AND ACCRETION PROCESSES

Relativity and black holes

Spherical accretion on BHs and why do we need supermassive BHs

Disk accretion on BHs:

geometrically-thin and thick disks: ADAF, ADIOS, CDAF, etc.

The central engine of AGN

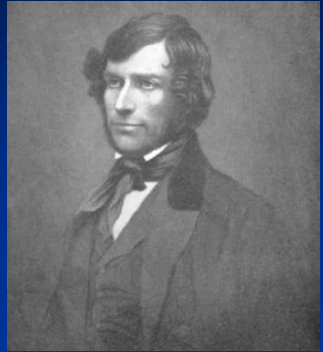
BLACK HOLES

❖ First mentioning of a black hole in history (1783):

If the semi-diameter of a sphere of the same density as the Sun were to exceed that of the Sun in the proportion of 500 to 1, a body falling from an infinite height towards it would have acquired at its surface greater velocity than that of light, and consequently supposing light to be attracted by the same force in proportion to its *vis inertiae*, with other bodies, all light emitted from such a body would be made to return towards it by its own proper gravity.

John Michell (1724-1793)

English clergyman and natural philosopher



John Michell



Karl Schwarzschild

$$\frac{1}{2} v^2 = \frac{GM}{R}$$



are there objects with $\frac{2GM}{Rc^2} \geq 1$?

Laplace (1896) in 1st and 2nd edition of his book, then removed this note....

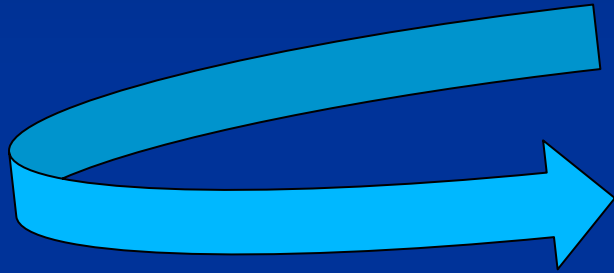
Karl Schwarzschild (1916) in a letter to Einstein from the front....

1st nontrivial stationary solution to Einstein eqs.

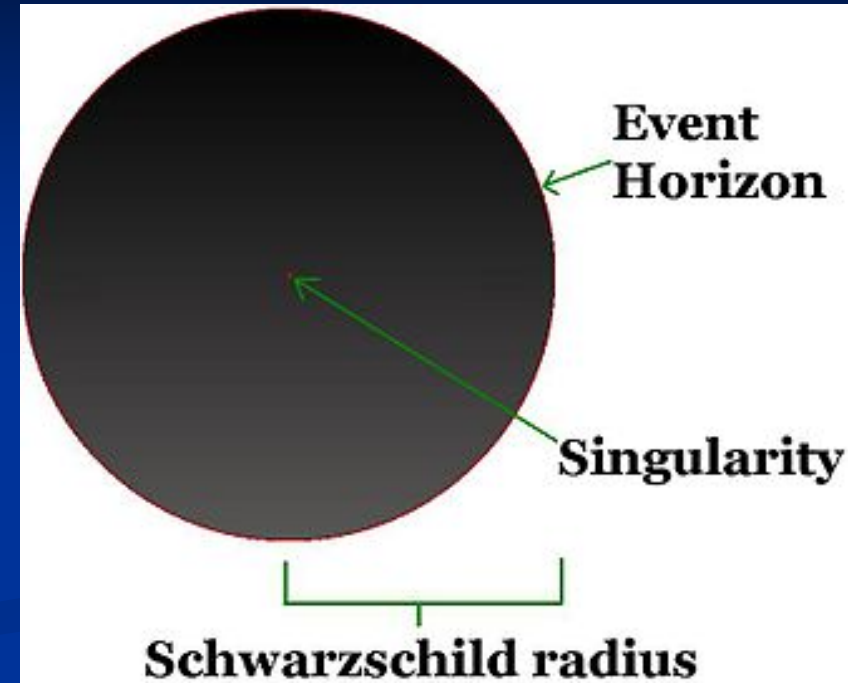


BLACK HOLES

A black hole is completely specified by their
masses M
angular momentum J
charge Q (likely = 0)



Black holes have no hair!
theorem by J.A. Wheeler



❖ **Schwarzschild black hole:** $J=0$, $Q=0$

→ spherically-symmetric with
radius $R_{\bullet} = 2GM/c^2$

→ smallest stable orbit at $R_{\min} = 3R_{\bullet}$

→ minimal orbital period for $M_{\bullet} \sim 10^{7-8} M_{\odot} \rightarrow$ few hours (variability)

Schwarzschild solution:

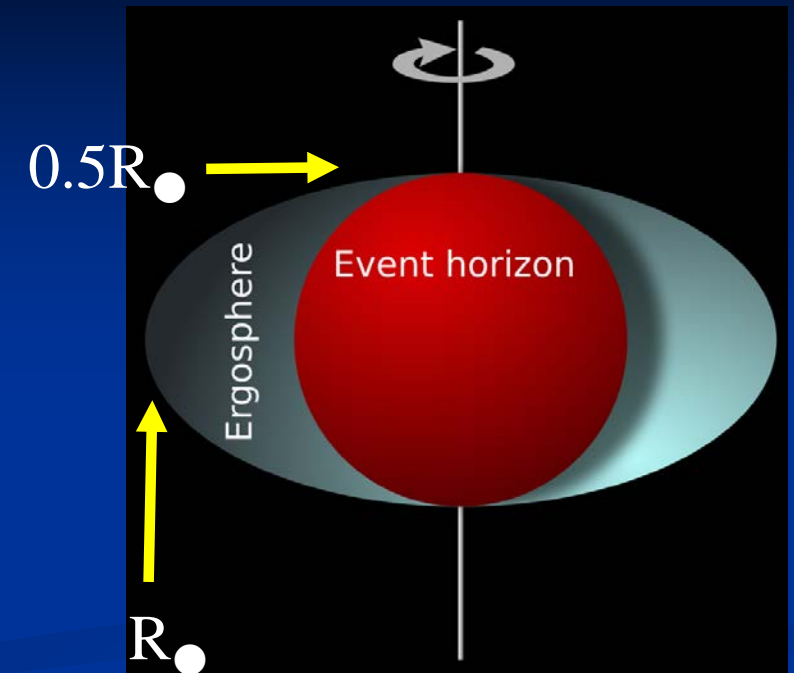
$$ds^2 = g_{\mu\nu} dx^{\mu} dx^{\nu} = - (1 - 2M/r) dt^2 + \frac{dr^2}{1 - 2M/r} + r^2 d\Omega^2 ,$$
$$d\Omega^2 = d\theta^2 + \sin^2 \theta d\varphi^2 ,$$

singularity!

BLACK HOLES

❖ Kerr (1963) black hole: axisymmetric \rightarrow parameter J

$$ds^2 = -dt^2 + (r^2 + a^2) \sin^2 \theta d\varphi^2 + \frac{2Mr(dt - a \sin^2 \theta d\varphi)^2}{r^2 + a^2 \cos^2 \theta} + (r^2 + a^2 \cos^2 \theta) \left(d\theta^2 + \frac{dr^2}{r^2 - 2Mr + a^2} \right).$$



Kerr black hole

1st law of black hole physics: the increase of the BH mass is the sum of all energies added to the BH

2nd law of black hole physics: the total area of the horizon cannot decrease

Lense-Thirring effect: dragging of inertial frames

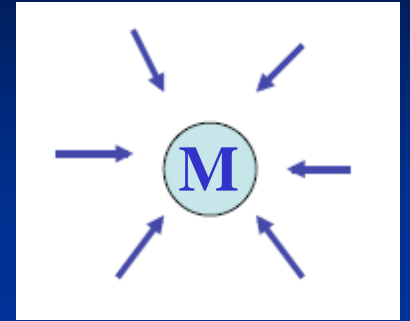
\rightarrow objects in the ergosphere cannot be at rest with respect to observer at ∞

ACCRETION ONTO BLACK HOLES

❖ Spherical accretion: Bondi-Hoyle solution

Steady-state spherical inflow under gravity (at rest at ∞)

→ mass conservation equation



$$\underline{\nabla} \cdot (\rho \underline{u}) = 0 \quad \text{eq.(1)}$$

$$\int_V \underline{\nabla} \cdot (\rho \underline{u}) dV = \int_S \rho \underline{u} \cdot d\underline{S} \quad \rightarrow \quad 4\pi r^2 \rho u = \text{constant} = \dot{M} \quad \text{eq.(2)}$$

← mass inflow rate

→ steady-state momentum (Euler) equation:

$$(\underline{u} \cdot \underline{\nabla}) \underline{u} = -\frac{1}{\rho} \underline{\nabla} p - \underline{\nabla} \psi \quad \text{eq.(3)}$$

point mass
gravity

$$u \frac{\partial u}{\partial r} = -\frac{1}{\rho} \frac{\partial p}{\partial r} - \frac{GM}{r^2} \quad \text{eq.(4)}$$

$$\frac{\partial}{\partial r} (r^2 \rho u) = 0 \quad \rightarrow \quad 2r\rho u + r^2 u \frac{\partial \rho}{\partial r} + r^2 \rho \frac{\partial u}{\partial r} = 0 \quad \rightarrow \quad -\frac{1}{\rho} \frac{\partial \rho}{\partial r} = \frac{2}{r} + \frac{1}{u} \frac{\partial u}{\partial r}$$

But

$$\frac{1}{\rho} \frac{\partial p}{\partial r} = \frac{1}{\rho} \frac{\partial p}{\partial \rho} \frac{\partial \rho}{\partial r} = c_s^2 \frac{1}{\rho} \frac{\partial \rho}{\partial r}$$

ACCRETION ONTO BLACK HOLES

❖ Spherical accretion: Bondi-Hoyle solution

eq.(4):
$$u \frac{\partial u}{\partial r} = -\frac{1}{\rho} \frac{\partial p}{\partial r} - \frac{GM}{r^2}$$

$$(u^2 - c_s^2) \frac{\partial(\ln u)}{\partial r} = \frac{2c_s^2}{r} \left(1 - \frac{GM}{2c_s^2 r}\right)$$

So at $r_s = GM/2c_s^2$ or $u = c_s$ u is a maximum/minimum \rightarrow sonic transition happens at r_s

$c_s = \text{const.} \rightarrow T$ determines the sonic point

density at the sonic point:
$$\rho_s = \frac{\dot{M}}{4\pi r_s^2 c_s}$$

Definition of accretion radius: $r_{\text{acc}} = \frac{2GM}{c_s^2}$ \rightarrow $r_{\text{acc}} = \frac{2GM}{c^2 + v^2}$ If M moving with speed v

ACCRETION ONTO BLACK HOLES

❖ Spherical accretion: Bondi-Hoyle solution

Insert r_{acc} into \dot{M}  $\dot{M} \sim \frac{4\pi\rho G^2 M^2_{\bullet}}{(c^2 + v^2)^{3/2}}$ accretion rate

$$\dot{M} \sim 6 \times 10^{-16} \left(\frac{M_{\bullet}}{1M_{\odot}} \right)^2 M_{\odot}/\text{yr}$$

for $T=10^4$ K
 $v=0$
 $\rho = 10^{-24}$ g/cm³

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❖ Eddington limit

For an AGN with observed bolometric luminosity $L \rightarrow$ estimate minimum M_{\bullet}
 \rightarrow spherically-symmetric accretion, fully ionized H

Flux at distance r

$$F = \frac{L}{4\pi r^2}$$

Corresponding radiation pressure on free electrons

$$P_{\text{rad}} = \frac{L}{4\pi r^2 c}$$

\rightarrow using minimum cross section (Thomson)
 $\sigma_T = 6.65 \times 10^{-25} \text{ cm}^2$

Resulting outward radiation force on a single electron:

$$f_{\text{rad}} = \frac{L\sigma_T}{4\pi r^2 c}$$

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❖ Eddington limit

Balancing by gravity per proton (WHY?): $f_{\text{grav}} = \frac{GMm_p}{r^2}$

$$L = \frac{4\pi Gcm_p}{\sigma_T} M = 1.3 \times 10^{38} \left(\frac{M}{M_{\odot}} \right) \text{ erg/s}$$

The Eddington luminosity

Inverting this formula
and using AGN luminosity:

$$M_{\bullet} = 8 \times 10^5 \left(\frac{L}{10^{44} \text{ erg/s}} \right) M_{\odot}$$

this is minimum mass

Need supermassive BHs to explain the AGN luminosity! → SMBH



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❖ Fueling AGN To produce

Need

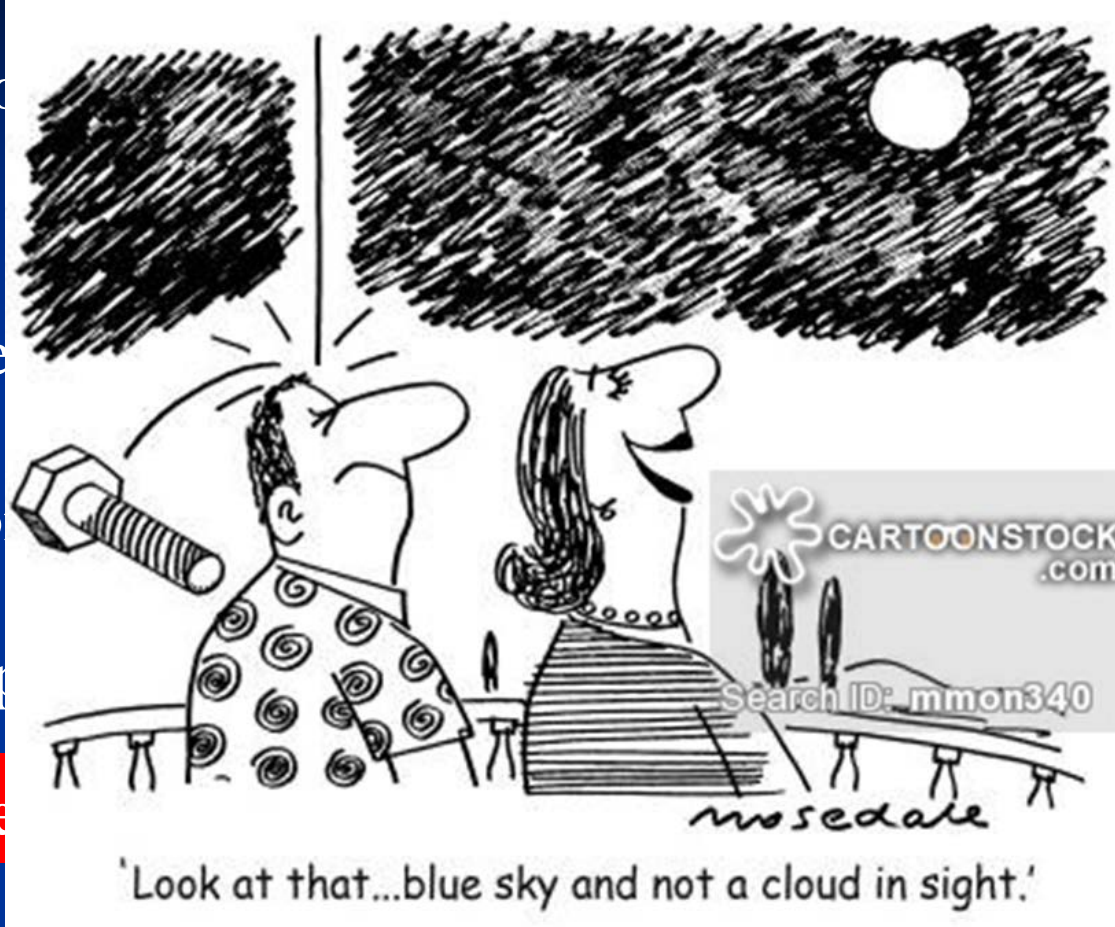
Define efficiency of e

Mass δm accretes from

Available energy to sp

This is an upper

Energy/mass: $E_{\text{pot}} = \frac{GM}{r}$



s

this gas must be accreted?

$$L = \eta \dot{M} c^2$$

$$= \frac{GM \dot{M}}{r}$$

radiation!

→ for neutron star ($1 M_{\odot}$, 10 km) $\sim 1.4 \times 10^{20}$ erg/gm
 → for black hole ($1 M_{\odot}$, 3 km) $\sim 4.6 \times 10^{20}$ erg/gm



but no hard surface! How can it radiate?

ACCRETION ONTO BLACK HOLES

❖ Spectra of AGN: two options

Energy of each proton is turned directly into heat by a shock at the surface or horizon:

$$\frac{GM}{r} \rightarrow \frac{3kT}{m_p} \rightarrow T_s \sim 1 \times 10^{12} \text{ K} \quad \text{for neutron star}$$
$$\rightarrow \sim 3 \times 10^{12} \text{ K} \quad \text{for any mass BH}$$

Energy of each proton is thermalized and radiated away as a blackbody
(at Eddington luminosity)

$$L_E = 4\pi r^2 \sigma T^4$$
$$\rightarrow T_{bb} \sim 10^7 \text{ K} \quad \text{for neutron star}$$
$$\sim 10^5 \text{ K} \quad \text{for SMBH of } 10^8 M_\odot \rightarrow R_s = 2GM_\bullet / c^2 \sim 3 \times 10^{13} \text{ cm}$$

**SMBH are expected to radiate from optical/UV \rightarrow X-rays \rightarrow γ rays !
Great fit to observations of AGN!**



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❖ Fueling AGN

If $L \sim L(\text{Eddington}) \rightarrow$ SMBH grows exponentially!

$$L = \frac{GM_{\bullet} \dot{M}}{r} \iff L_{\text{edd}} = \frac{4\pi G c m_p}{\sigma_T} M_{\bullet}$$

$$\frac{1}{M_{\bullet}} dM_{\bullet} = \text{const.} \times dt \quad \rightarrow \quad t_{\text{Sal}} = \frac{\eta \sigma_T c}{4\pi G m_p} \sim 4.5 \eta_{0.1} 10^7 \text{ yr}$$

$M_{\bullet} = M_{0\bullet} e^{t/t(\text{Sal})}$

Salpeter (1964) *e*-folding time for the BH growth at the Eddington rate

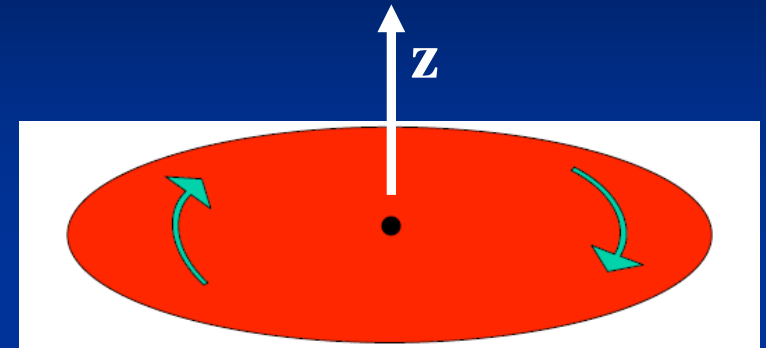


ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** Shakura-Sunyaev-Novikov-Thorne solution \rightarrow geometrically-thin disks

$$\Sigma = \int_{-\infty}^{\infty} \rho dz \approx 2H \langle \rho \rangle$$

Σ = surface density of a disk
with a half-thickness H
in **cylindrical** coordinates R, φ, z



accretion disks are universal
mechanism to get rid of J

$v_{\varphi} = v_K = (GM_{\bullet}/R)^{1/2}$ rotation velocity is Keplerian
 \rightarrow disk is supported by rotation only



radial pressure gradient \rightarrow neglect



For gas to move inward $\rightarrow \mathbf{J}/M = \mathbf{R} \times \mathbf{v} = (GM_{\bullet}R)^{1/2}$ must move out!
 \rightarrow needs (coefficient of kinematic) viscosity ν !

$\nu \sim v_T \lambda$ \rightarrow thermal velocity x mean free path

\rightarrow assume viscous torque $G(R)$ between neighboring disk rings

ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** Shakura-Sunyaev-Novikov-Thorne solution \rightarrow geometrically-thin disks

Assume $G(R)$ viscous torque between neighboring disk rings:

$$G(R) = 2\pi R \Sigma R^2 \nu \Omega' \quad \text{where} \quad \Omega' = d\Omega/dR$$

$$R d\Omega/dR \leftarrow \text{shear}$$

$$\Omega = (GM_{\bullet}/R^3)^{1/2} \rightarrow \text{angular velocity in Keplerian disk}$$

Net torque on a disk ring between R and $R+\Delta R$ is

$$G(R + \Delta R) - G(R) = \frac{\partial G}{\partial R} \Delta R$$

eq.(5)



analog of thin accretion disk



Torque does work at a rate:

$$\Omega \frac{\partial G}{\partial R} \Delta R = \left[\underbrace{\frac{\partial}{\partial R} (G\Omega)}_{\text{transport of rotational energy}} - \underbrace{G\Omega'}_{\text{dissipation per unit area}} \right] \Delta R \quad \text{eq.(6)}$$

transport of rotational energy

dissipation per unit area

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❖ **Disk accretion:** geometrically-thin disks \rightarrow viscous torque

Now, assume that the gas in the disk has a small radial velocity v_R

eq.(7) equation of the mass conservation in the disk (continuity eq.)

$$R \frac{\partial \Sigma}{\partial t} + \frac{\partial}{\partial R} (R \Sigma v_R) = 0$$

eq.(8) equation of J conservation in the disk

$$R \frac{\partial}{\partial t} (\Sigma R^2 \Omega) + \frac{\partial}{\partial R} (R \Sigma v_R R^2 \Omega) = \frac{1}{2\pi} \frac{\partial G}{\partial R}$$

combine

eq.(9)

$$R \frac{\partial \Sigma}{\partial t} = -\frac{1}{2\pi} \frac{\partial}{\partial R} \left[\frac{1}{(R^2 \Omega)'} \frac{\partial G}{\partial R} \right]$$

$G(R) = 2\pi R \Sigma R^2 \nu \Omega'$

$$\frac{\partial \Sigma}{\partial t} = \frac{3}{R} \frac{\partial}{\partial R} \left[R^{1/2} \frac{\partial}{\partial R} (\nu \Sigma R^{1/2}) \right]$$

eq.(10)

$$u_R(R, t) = -\frac{3}{\Sigma R^{1/2}} \frac{\partial}{\partial R} (\nu \Sigma R^{1/2})$$

insert into eq.(7)

ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ Disk accretion: geometrically-thin disks \rightarrow timescales

$$\frac{\partial^2}{\partial R^2} \longrightarrow \frac{1}{R^2}$$

$$t_{\text{acc}}^{-1} = \frac{1}{\Sigma} \frac{\partial \Sigma}{\partial t}$$

$t_{\text{visc}} \sim R^2/\nu$ viscous timescale is extremely long! Need “anomalous” viscosity!

$t_{\text{dyn}} \sim R/v_K \sim \Omega^{-1} \sim (R^3/GM_{\bullet})^{1/2}$ dynamical timescale

$t_{\text{th}} \sim \Sigma c_s^2/D(R) \sim R^3 c_s^2/GM_{\bullet} \nu \sim \frac{R^2}{\nu} \frac{c_s^2}{v_K^2} \sim \frac{H^2}{R^2} t_{\text{visc}}$



$$t_{\text{dyn}} < t_{\text{th}} < t_{\text{visc}}$$

ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** geometrically-thin disks → example

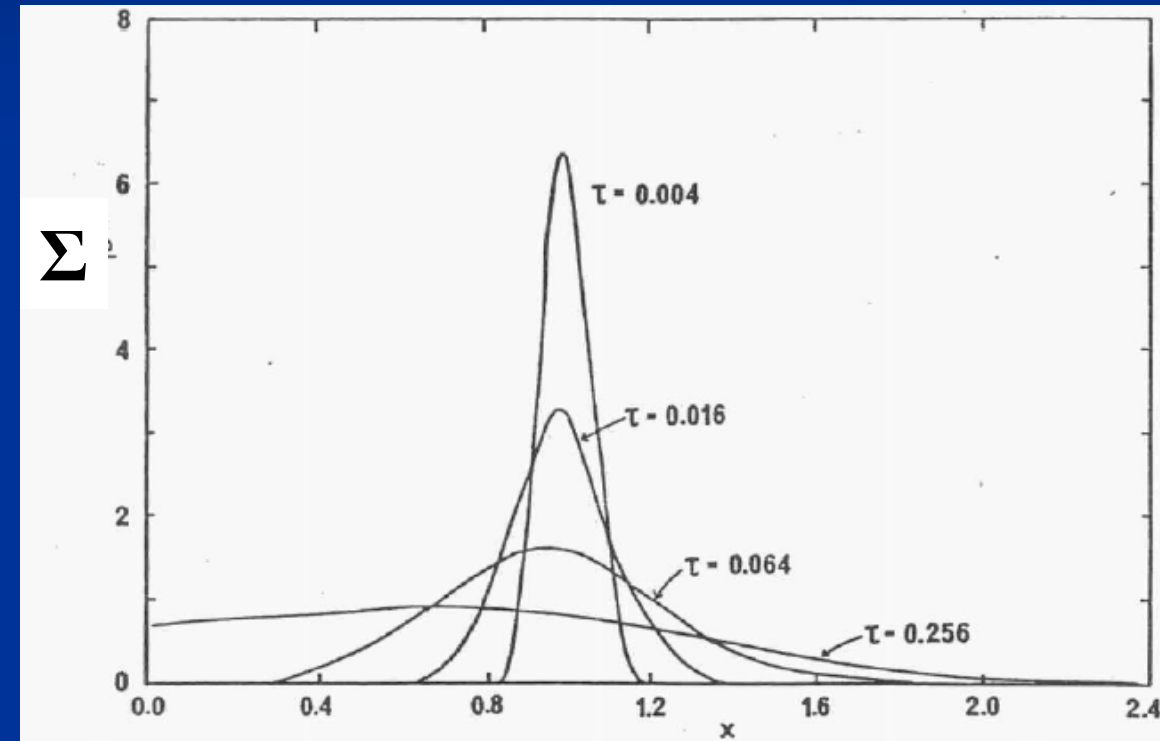
Assume an infinitesimally thin ring with mass m and radius R_0 → $x=R/R_0$; $\tau = t (12\nu/R_0^2)$

$$\Sigma(R, t = 0) = \frac{m\delta(R - R_0)}{2\pi R_0}$$

solution

$$\Sigma(x, \tau) = \frac{m}{\pi R_0^2} \tau^{-1} x^{-1/4} \exp\left[-\frac{1+x^2}{\tau}\right] I_{1/4}\left(\frac{2x}{\tau}\right)$$

where $I_{1/4}$ is modified Bessel function



$x=R/R_0$

viscous evolution of thin ring

**At later time, the ring moves inward, but has a long tail to large R
→ most material is accreted, but some escapes with large J**

ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** geometrically-thin disks \rightarrow steady-state

Steady-state radial momentum conservation equation:

$$u_R \frac{\partial u_R}{\partial R} - \frac{u_\phi^2}{R} + \frac{1}{\rho} \frac{\partial P}{\partial R} + \frac{GM_\bullet}{R^2} = 0$$

$$\frac{1}{\rho} \frac{\partial P}{\partial z} = -\frac{GM_\bullet}{R^3}$$

vertical hydrostatic equilibrium $\rightarrow H \sim c_s (GM_\bullet/R^3)^{-1/2} \sim c_s \Omega^{-1} \sim (c_s/v_\phi) R$

$$\dot{M} = -2\pi R \Sigma u_R$$

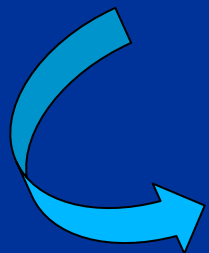
mass conservation \rightarrow mass inflow rate (accretion rate)

$$\partial \Sigma / \partial t = 0$$

$$-\nu \Sigma \frac{\partial \Omega}{\partial R} = -\Sigma u_R \Omega - \frac{C}{2\pi R^3}$$

integrating equation of J conservation

$$\rightarrow C = \dot{M} (GM_\bullet R_0)^{1/2} \text{ - constant of integration}$$



$$\nu \Sigma = \frac{\dot{M}}{3\pi} \left[1 - \left(\frac{R_0}{R} \right)^{1/2} \right]$$

where $R_0 = 3R_\bullet$ is the innermost stable orbit around BH

ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** geometrically-thin disks → emission

Dissipation rate of rotational kinetic energy per per unit time per unit area

$$D(R) = \frac{G\Omega'}{4\pi R} = \frac{1}{2}v\Sigma(R\Omega')^2 = \frac{9}{8}v\Sigma \frac{GM}{R^3}$$

→
for Keplerian disk

$$D(R) = \frac{3GM\dot{M}}{4\pi R^3} \left[1 - \left(\frac{R_0}{R} \right)^{1/2} \right]$$

no dependency on viscosity!

$$L_{\text{disk}} = \int_{R_0}^{\infty} D(R) 2\pi R dR = \frac{1}{2} \frac{GM\dot{M}}{R_0}$$

only $0.5E_{\text{pot}}$ → the rest is sucked in by the BH

If accretion disk optically thick (blackbody) → emissivity $B(T) \sim \sigma T^4$ → $T \sim R^{-3/4}$

Accretion disk spectrum:

$$S_\nu \propto \int_{R_{\text{in}}}^{R_{\text{out}}} B_\nu [T(R)] 2\pi R dR$$

1973A&A....24..337S

Astron. & Astrophys. 24, 337–355 (1973)

Black Holes in Binary Systems. Observational Appearance

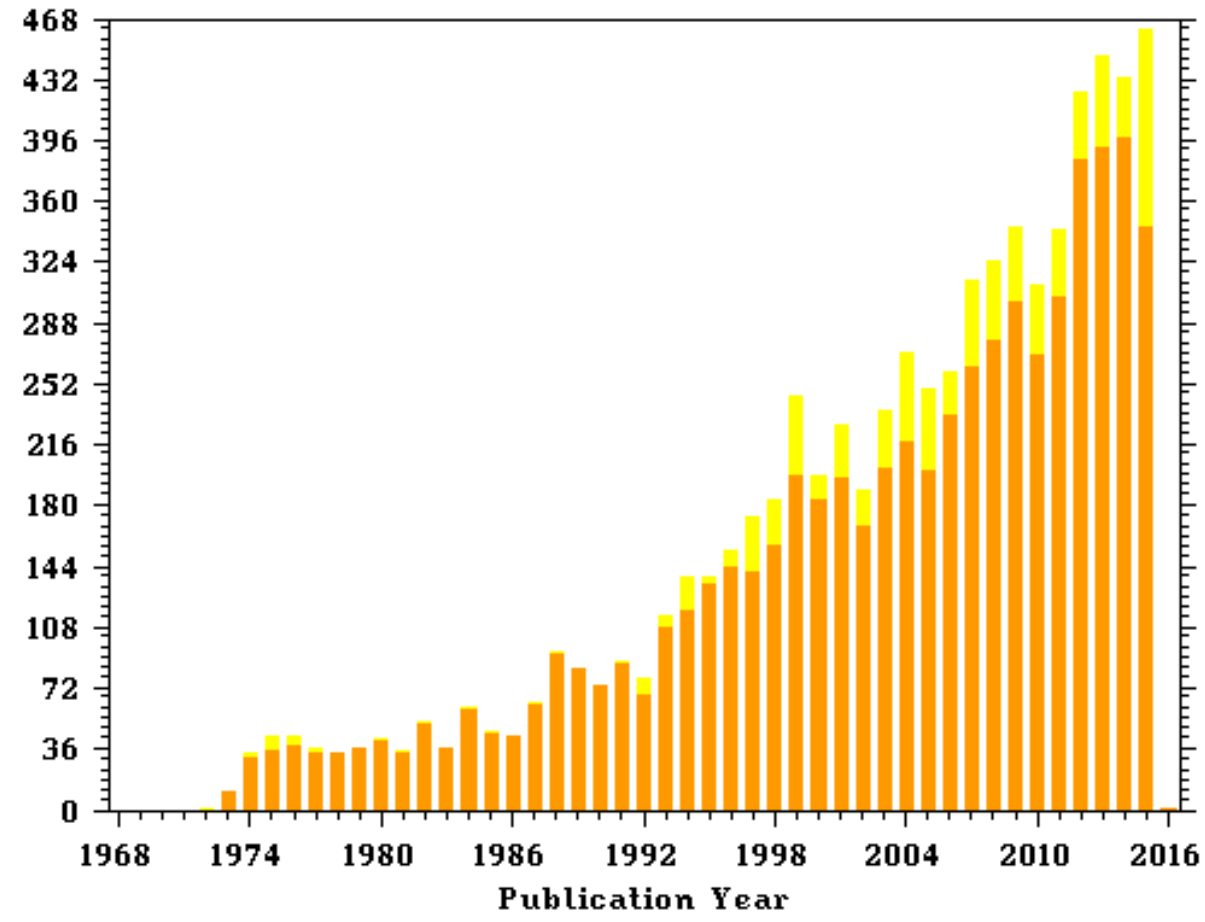
N. I. Shakura
Sternberg Astronomical Institute, Moscow, U.S.S.R.

R. A. Sunyaev
Institute of Applied Mathematics, Academy of Sciences, Moscow,

Received June 6, 1972

Summary. The outward transfer of the angular momentum of the accreting matter leads to the formation of a disk around the black hole. The structure and emission spectrum of the disk depend, mainly on the rate of matter inflow \dot{M} into the disk at its external boundary. The dependence on the efficiency of mechanical angular momentum transport (connected with the presence of a magnetic field and turbulence) is weaker. If $\dot{M} < 3 \cdot 10^{-8} M_{\odot} \text{yr}^{-1}$ the disk around the black hole

Citations/Publication Year for 1973A&A....24..337S



Unrefereed
Refereed
Total citations: 7204
Total refereed: 6317

ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** geometrically-thin disks \rightarrow emission

Viscosity responsible for energy-to-radiation conversion

$$S_\nu \propto \int_{R_{\text{in}}}^{R_{\text{out}}} B_\nu [T(R)] 2\pi R dR$$

$$\nu = \alpha c_s H \quad (\text{Shakura \& Sunyaev 1973})$$

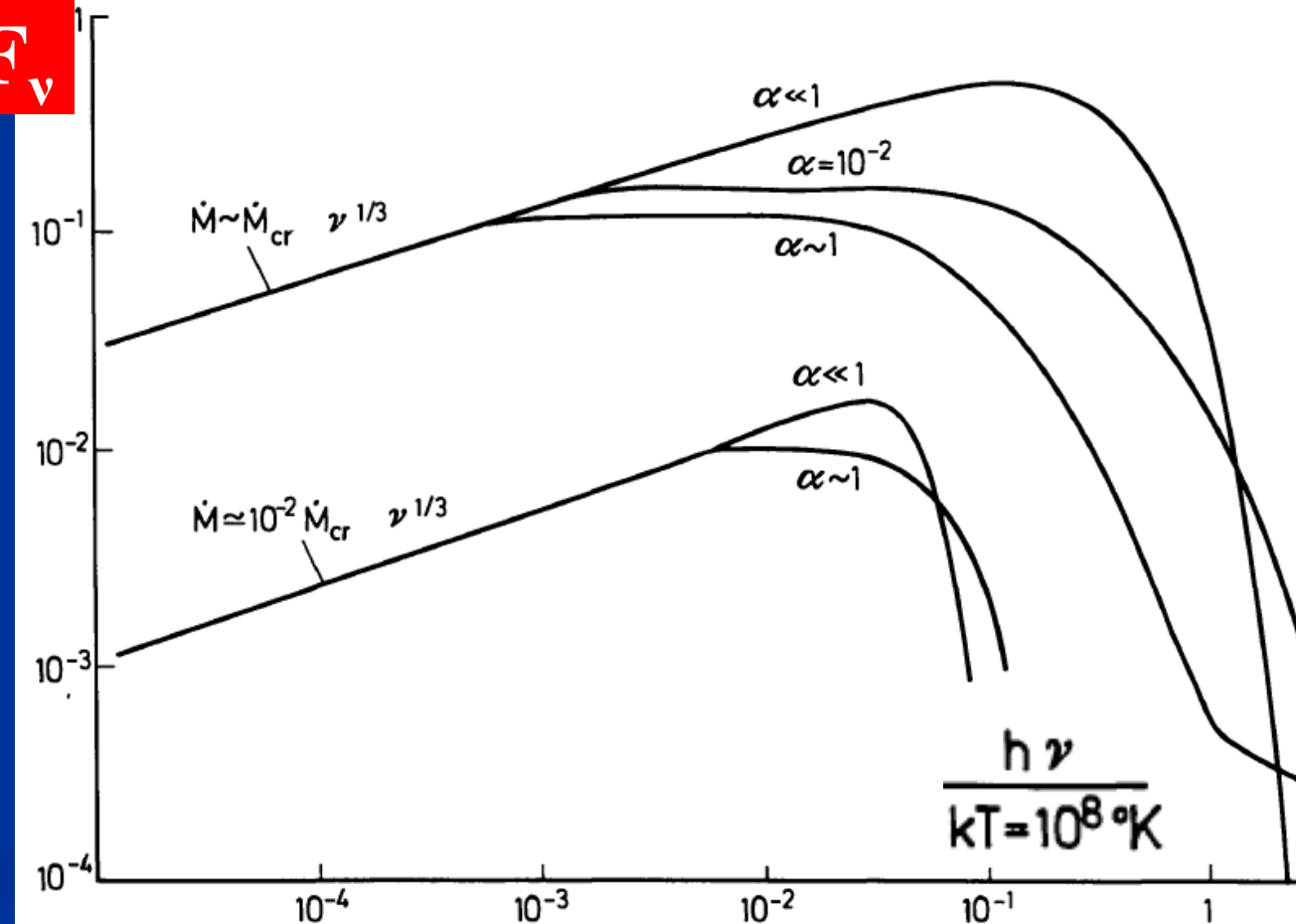
\rightarrow definition of α - viscosity

$\rightarrow [\nu] = \text{cm}^2/\text{s}$ α - dimensionless

Remember: $\nu \sim \lambda v_T \rightarrow \alpha c_s H$

$\lambda \leq H$ and $v_T \leq c_s \rightarrow \alpha \leq 1$

F_ν



Spectra of geometrically-thin, optically-thick accretion disks 21

ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** geometrically-thin disks \rightarrow spin up of the BH

Accretion of angular momentum J

$$\dot{J} \sim \dot{M} (GM_{\bullet} R_0)^{1/2}$$

photon emission limits J for the BH

Dimensionless angular momentum

$$a = \frac{cJ}{GM_{\bullet}^2}$$

where $0 \leq a \leq 1$

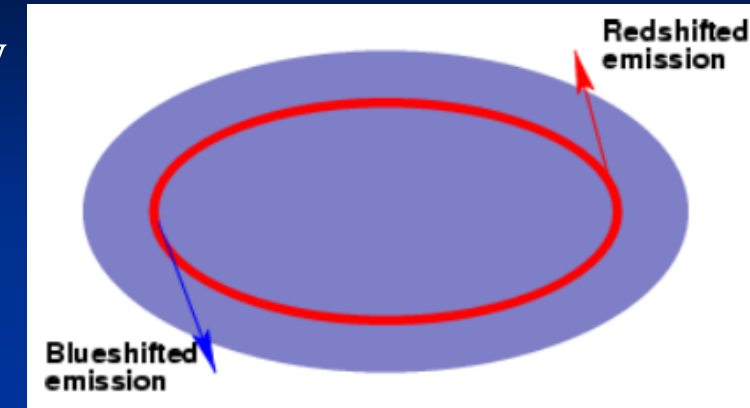
ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** evidence for SMBHs from X-ray spectroscopy

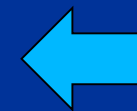
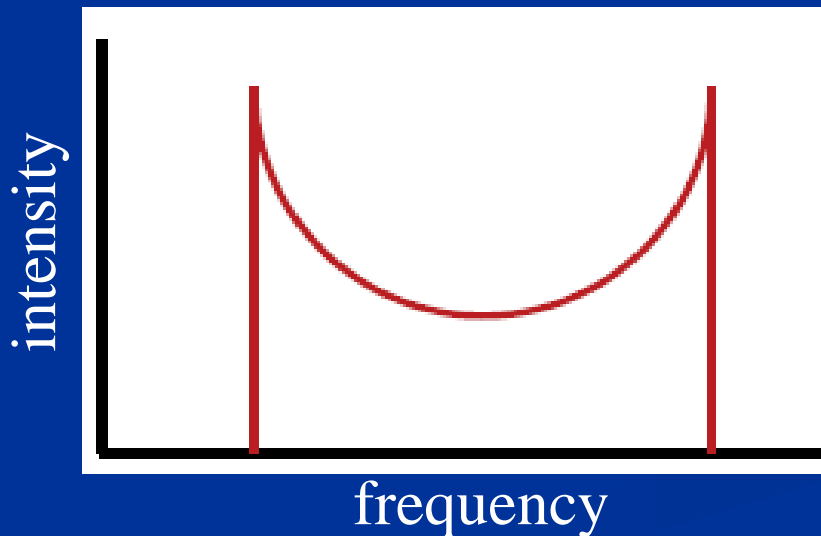
Measuring spectral line profiles from the inner disk

Fe lines in X-rays

Newtonian case ONLY!



$$\frac{\Delta\nu}{\nu} = \frac{v_{\text{obs}}}{c}$$



double-horned line profile
from a single ring in the disk

ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** evidence for SMBHs from X-ray spectroscopy

Fe lines in X-rays

relativistic case → several effects

Transverse Doppler effect:

moving clock slows down →
observed ν is reduced compared to
the rest frame by $(1 - v^2/c^2)^{-1/2}$

Beaming:

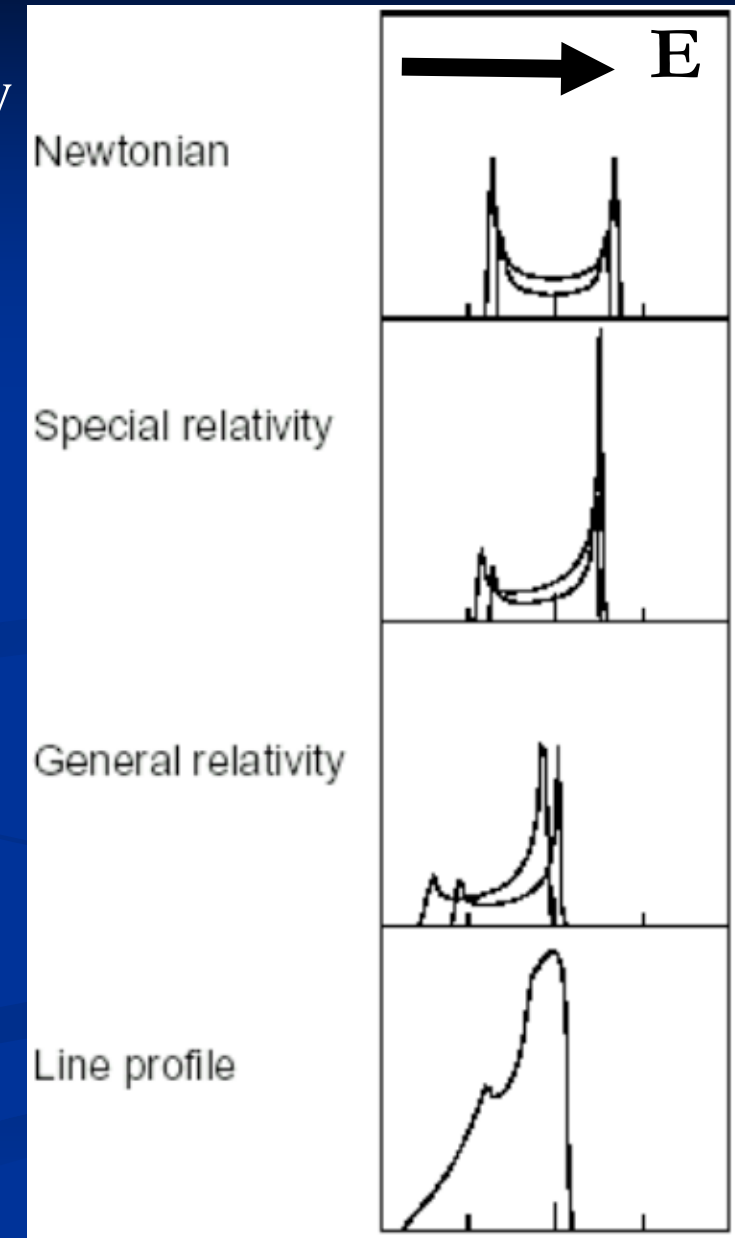
boosts blue wing of the line,
attenuates red wing

Gravitational redshift:

more shift to lower energies

**Integrate over all radii
and predict:**

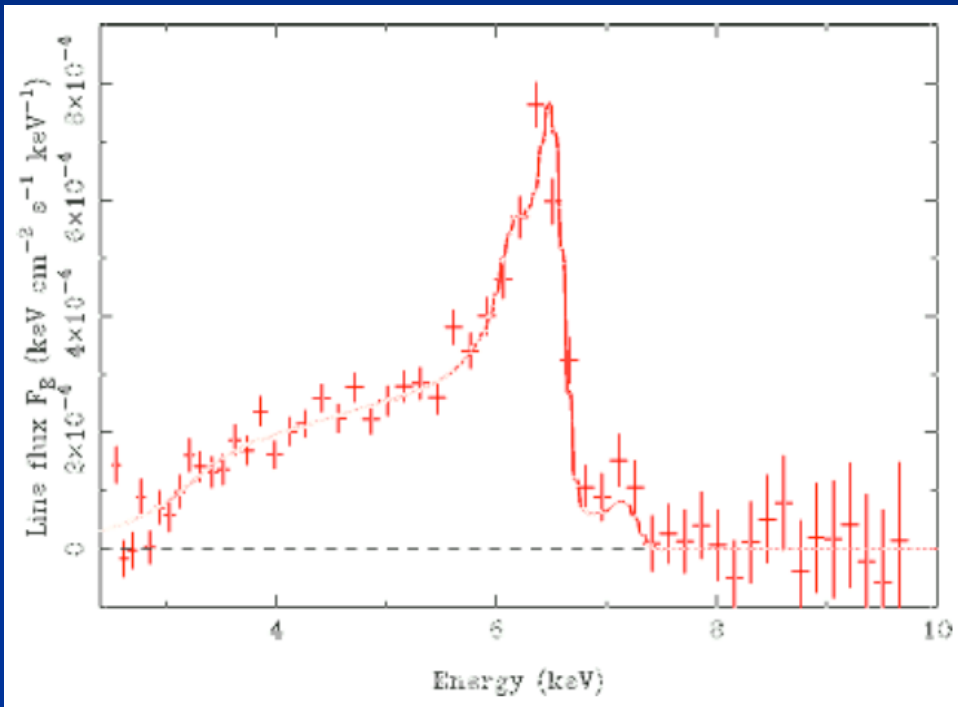
broad, asymmetric line profile
with a sharp cutoff at high E



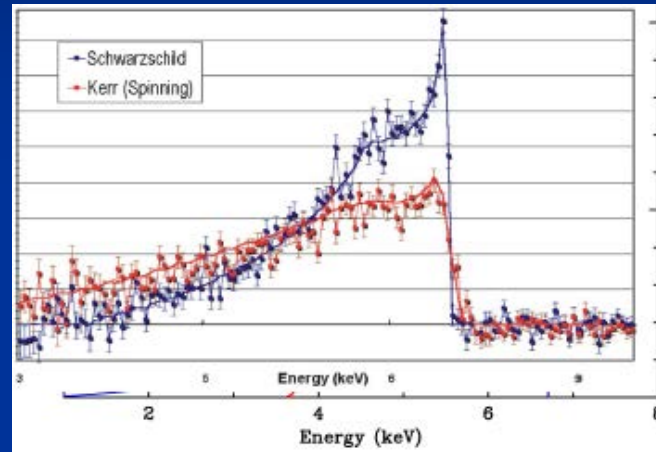
ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** evidence for SMBHs from X-ray spectroscopy

Fe lines in X-rays → observations

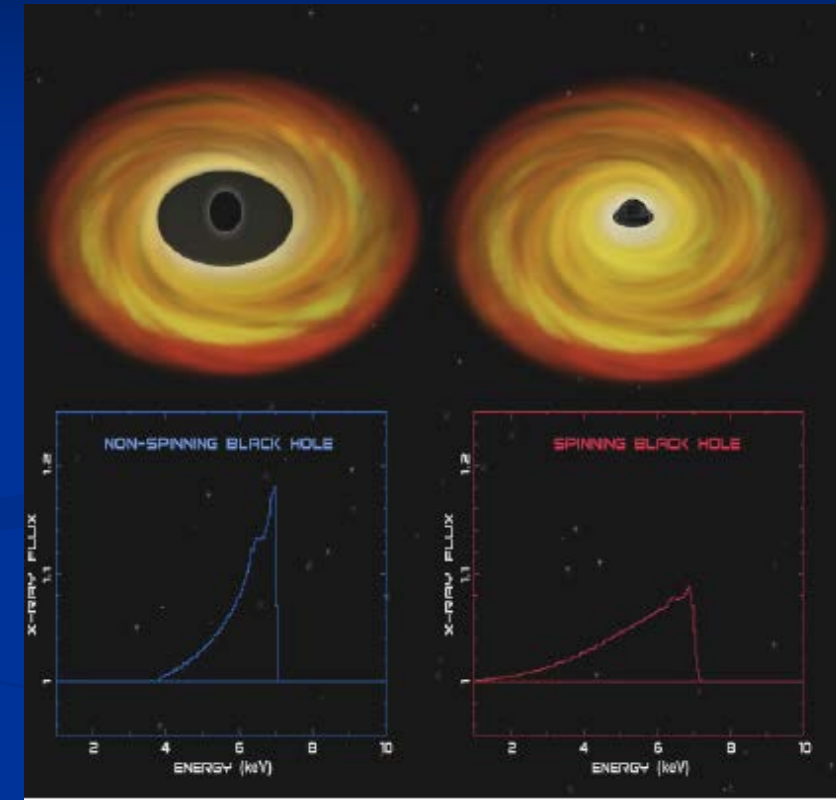


Fe line profile for
Seyfert galaxy
MCG-6-30-15
using XMM-Newton



Fe line profile: often extremely broad
→ detailed modeling of the line shape
→ rapidly spinning SMBH

Best proof to date of presence of SMBHs in AGN!

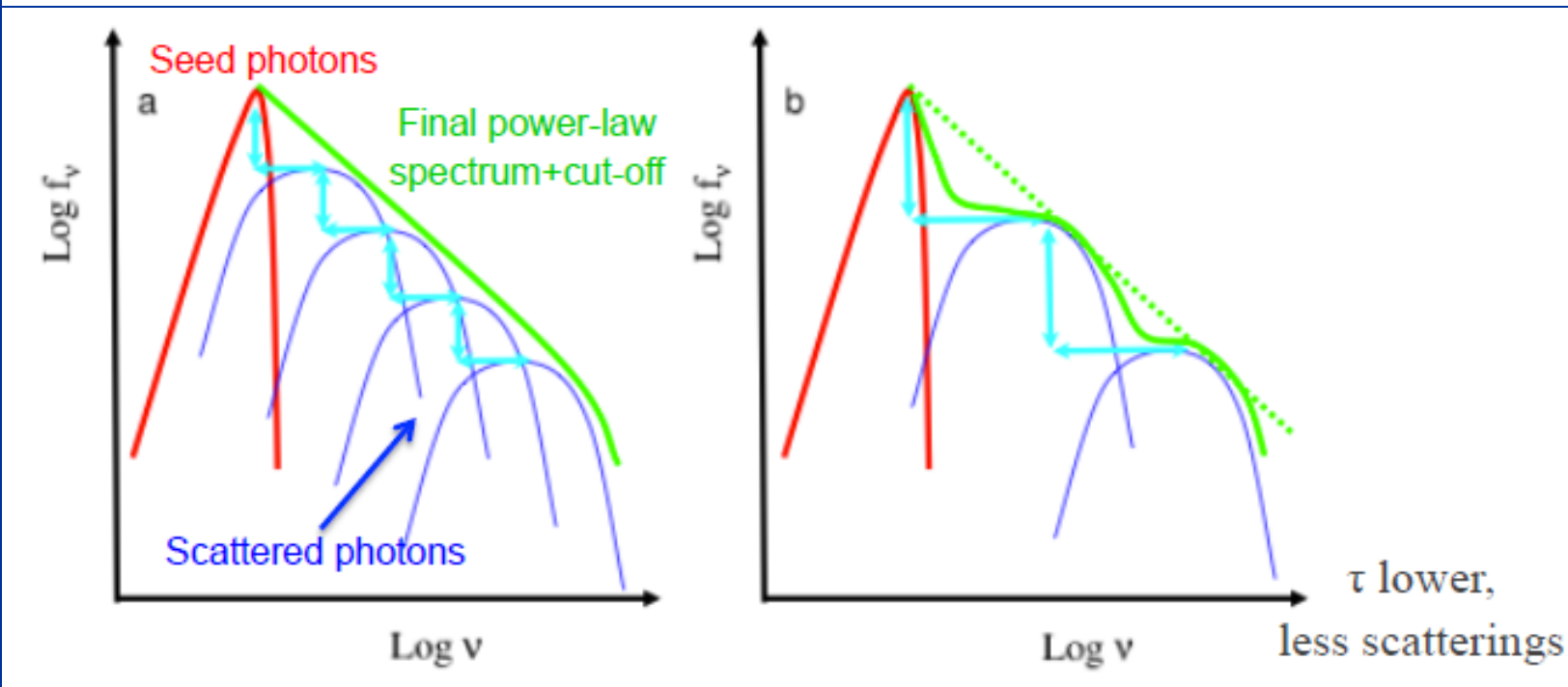


ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ Disk accretion: comptonization

Seed photons are up-scattered, then become the “new” seed photons for following scatterings → the overall spectrum resembles that of a powerlaw

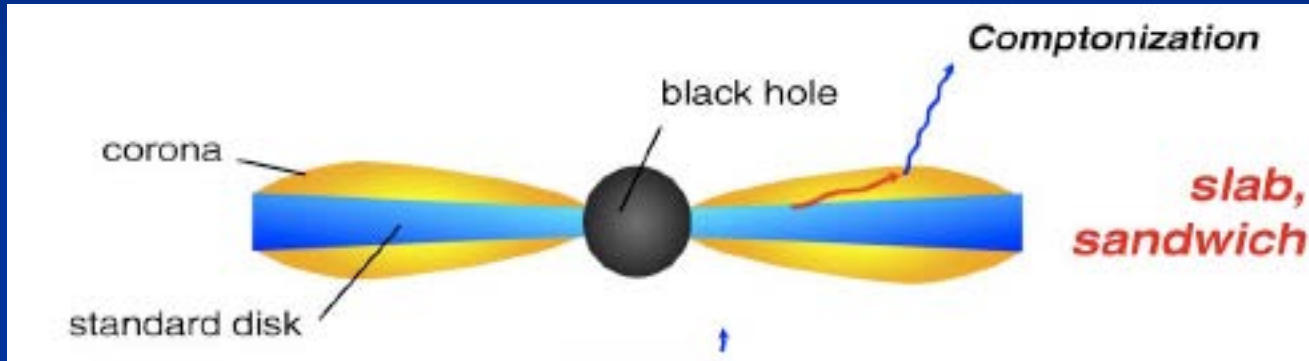
Thermal Comptonization: electrons have a Maxwellian distribution. Cut-off in the powerlaw when the process of transferring energy from electrons to photons is not efficient anymore ($E_{\text{cut-off}} \approx kT_{\text{electrons}}$)



ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** evidence for SMBHs from X-ray spectroscopy

Compton and inverse Compton effects



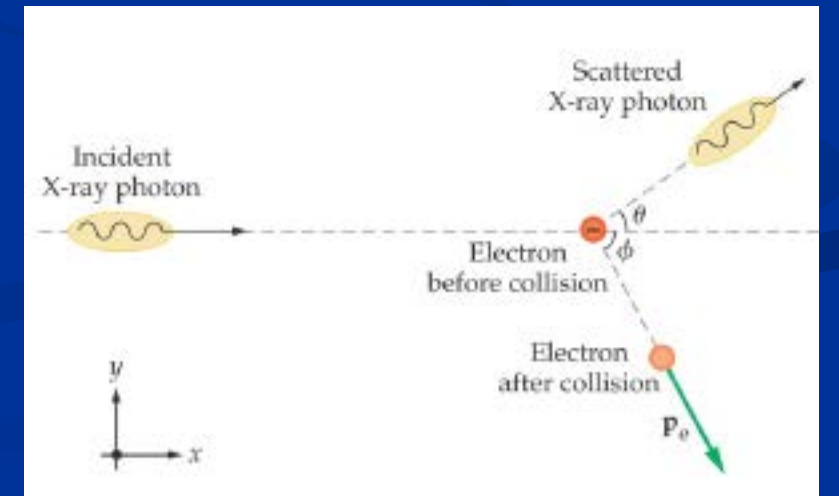
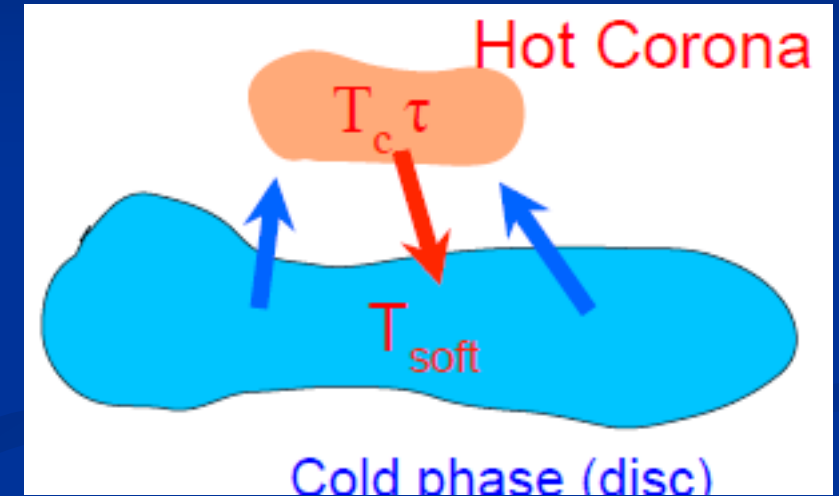
$$\Delta E = E' - E$$

$$\approx -\frac{E^2}{m_e c^2} (1 - \cos \theta)$$

For non-stationary electron:

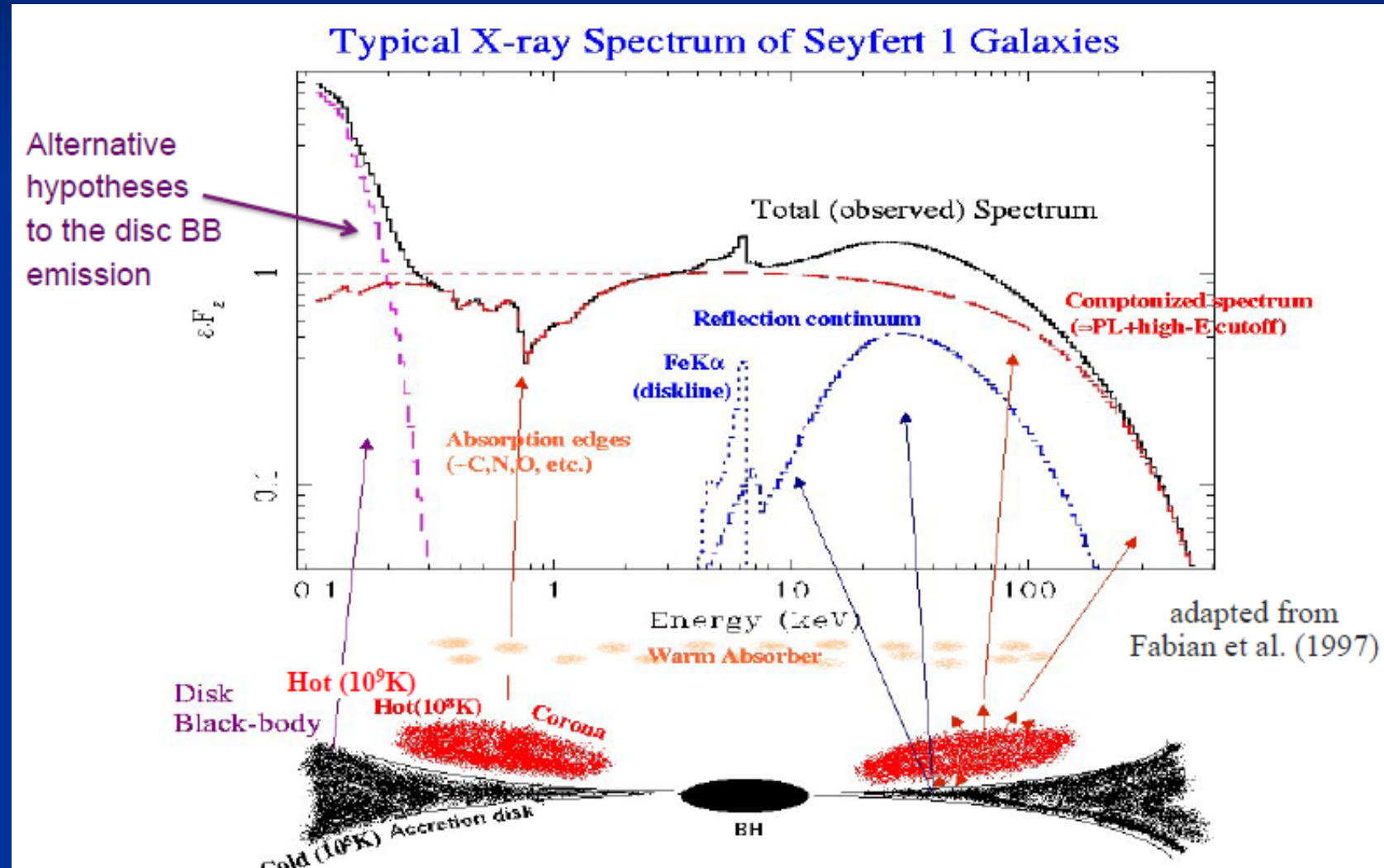
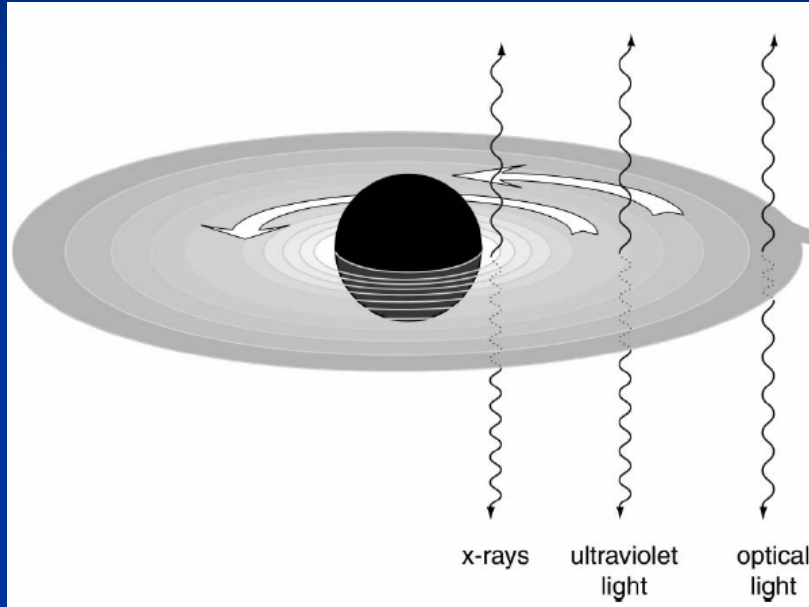
$\Delta E < 0 \rightarrow$ Compton

$\Delta E > 0 \rightarrow$ Inverse Compton

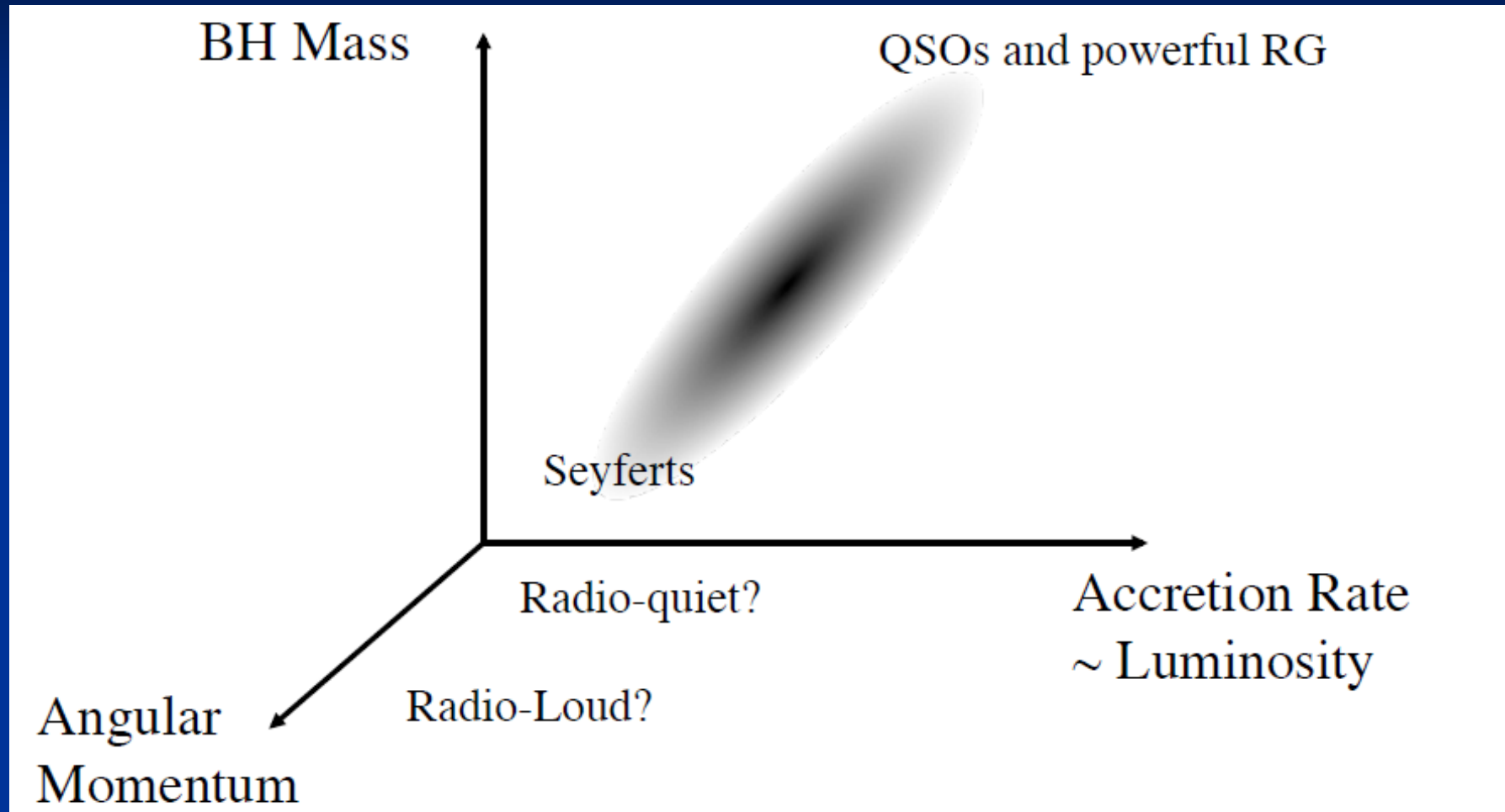


ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Disk accretion:** geometrically-thin disks \rightarrow thermal emission



AGN: PHYSICAL CLASSIFICATION



In addition, dependence on the viewing angle

EFFICIENCY OF ENERGY-TO-RADIATION CONVERSION

$$\diamond L = \eta \dot{M} c^2$$

Gas falls in to the last stable orbit at $3R_0$

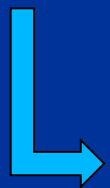
Efficiency of potential energy-to-radiation conversion
(Newtonian, but OK)

$$\eta = \frac{GM_{\bullet} \dot{M}}{6GM_{\bullet}/c^2 \dot{M}} \frac{c^{-2}}{\dot{M}} \sim 0.17$$

Actually, Schwarzschild BH: $\eta \sim 0.06$

Kerr BH: ~ 0.42

Taking $\eta \sim 0.1$



$$\dot{M} \sim 10^{46} \text{ erg/s} / 0.1 c^2 \sim 10^{26} \text{ g/s} \sim 2 M_{\odot}/\text{yr}$$



HST image of gas accreting
onto SMBH in elliptical galaxy
NGC 4261

EFFICIENCY OF ENERGY-TO-RADIATION CONVERSION

❖ **Slim disks:** non-Keplerian angular momentum

Shakura & Sunyaev disks: all dissipated energy is
Radiated locally \rightarrow viscous heating = radiative cooling



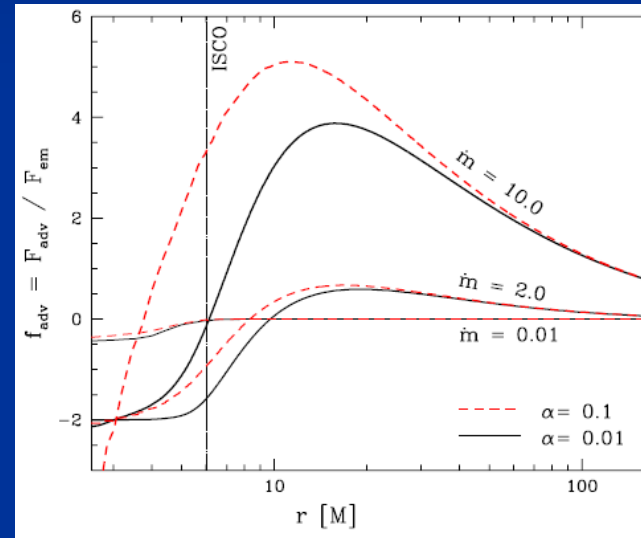
Good, if $\dot{M} \ll \dot{M}_{\text{Edd}}$
when $L > 0.3L_{\text{Edd}} \rightarrow v_R$ and H increase



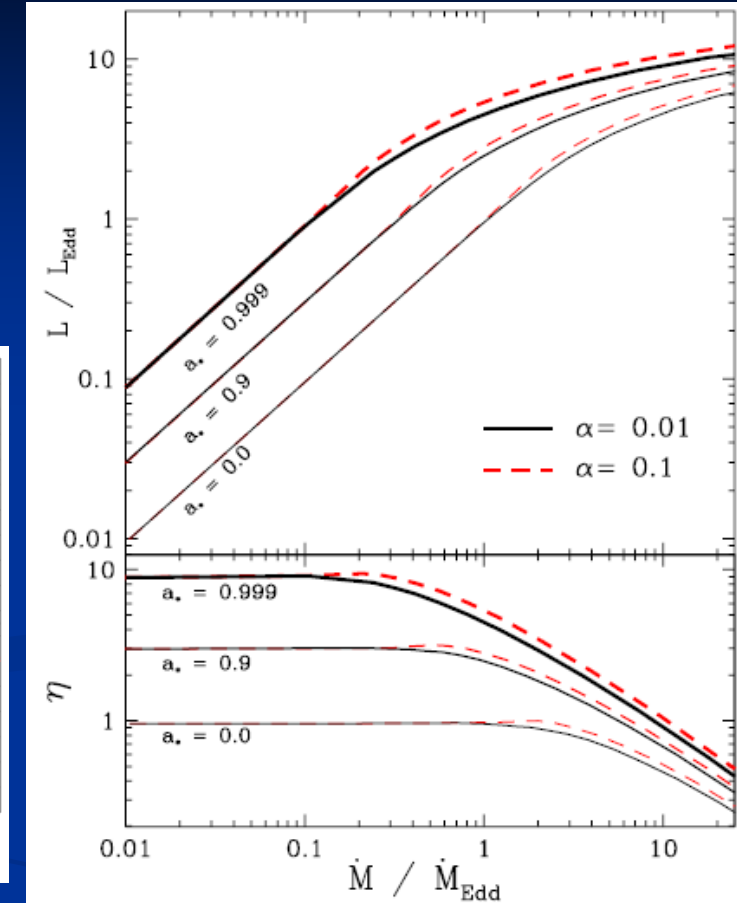
additional cooling: advection

Why?

\rightarrow photons have no time to escape



Advective-to-radiation
fluxes as a function of \dot{M}



Sadowski (2011)

**Still slim disks are luminous
and radiation efficient
 $\rightarrow \eta \sim 0.006 - 0.6$**

ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Thick disk accretion:** Advection Dominated Accretion Flow (ADAF)

Lightman, Eardley, Rees (1970s), Narayan & Yi (1990s), Abramowicz (1990s)

Nearly **all** viscosity-dissipated energy is carried (advected) into the SMBH and not radiated away \rightarrow dominated by gas pressure!

Two effects:

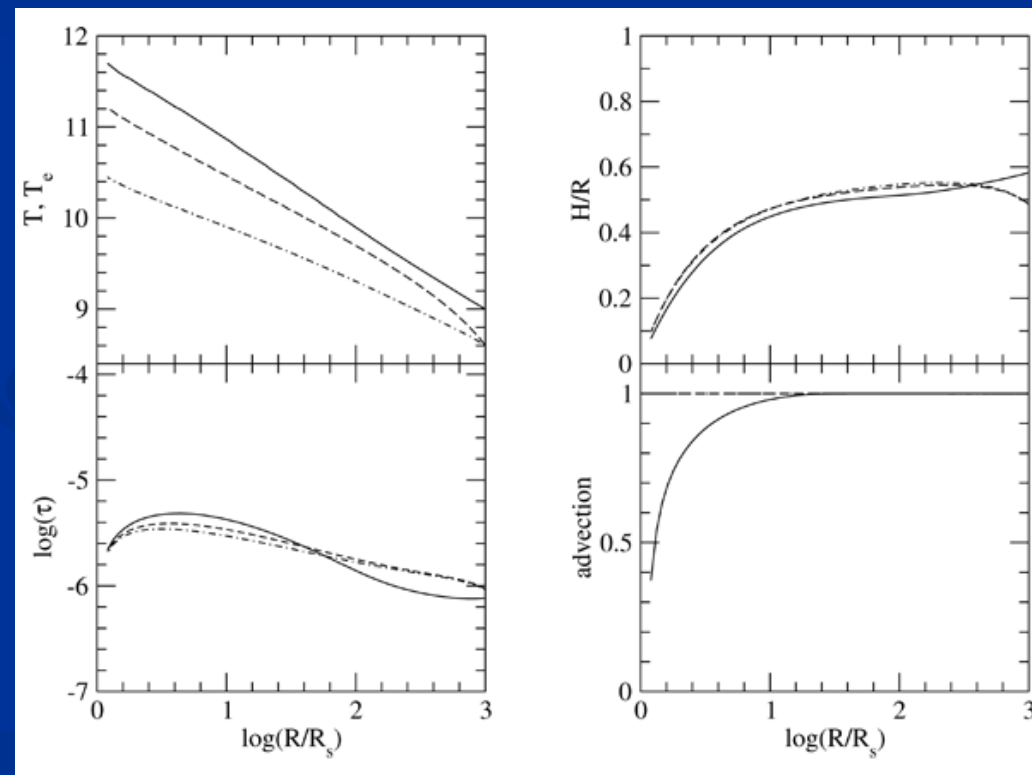
\rightarrow dissipated E cannot be radiated locally \rightarrow low L

\rightarrow rotation is not Keplerian, but....

Hot disk with $c_s \sim v_K$; $v_R \sim \alpha v_K (H/R)^2 \sim 0.1-0.3 v_K$

$$t_{\text{acc}} \sim R/v_R \sim t_{\text{ff}}/\alpha$$

Low-density gas \rightarrow very long cooling time \rightarrow optically-thin!



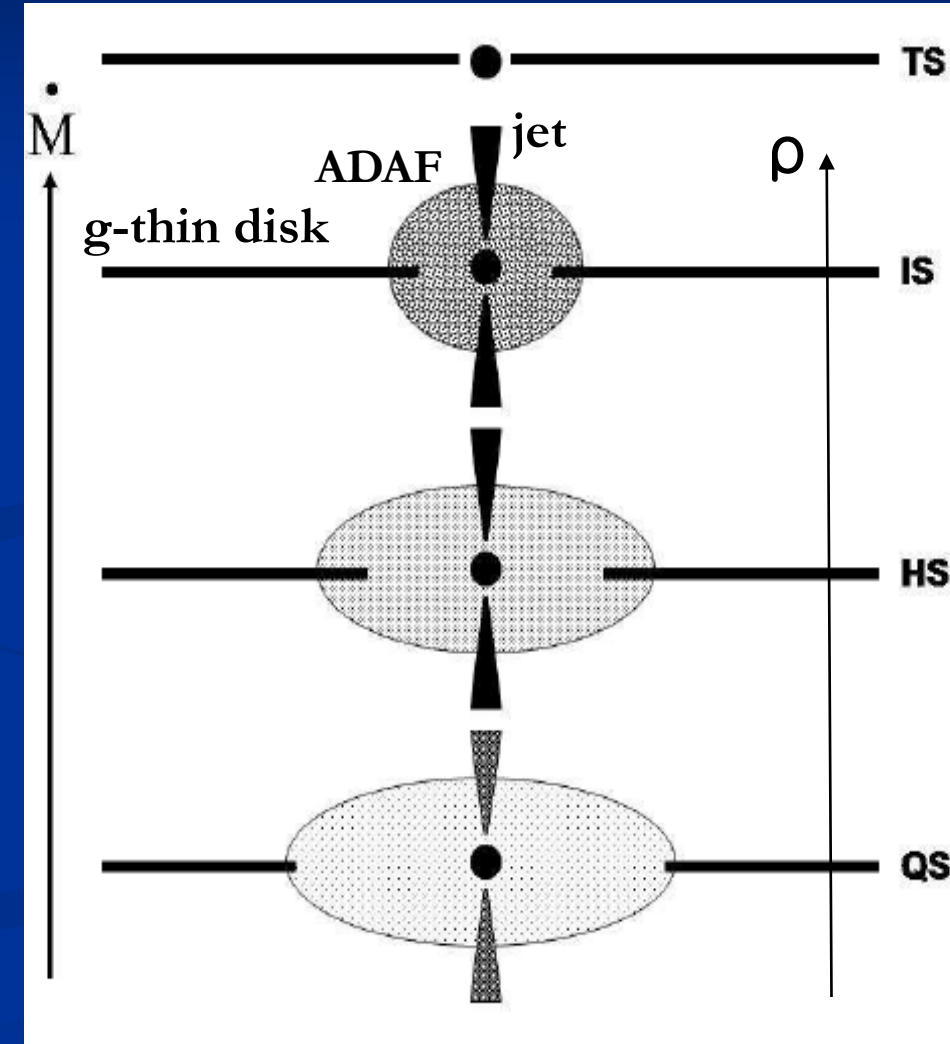
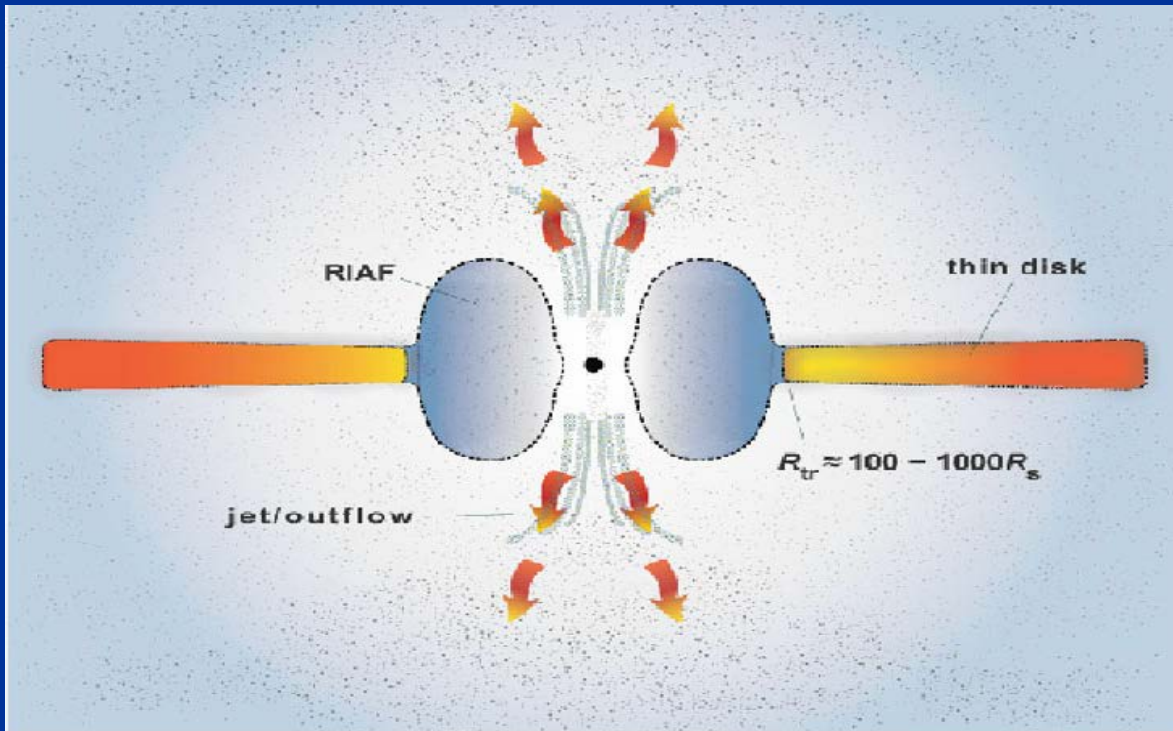
Abramowicz and Fragile (2013)

ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ Thick disk accretion: ADAF → Radiatively-Inefficient Accretion Flow (RIAF)

Low-luminosity AGN

$$L < 0.01 L_{\text{Edd}}$$



ACCRETION ONTO SUPERMASSIVE BLACK HOLES

- ❖ **Thick disk accretion:** Convection Dominated Accretion Flow (CDAF)
Quataert and Gruzinov (2002)

Much of viscosity-dissipated energy is carried
(advected) into the SMBH and not radiated away
→ convection carries energy to large R , but not to ∞
→ SMBH grows slowly!

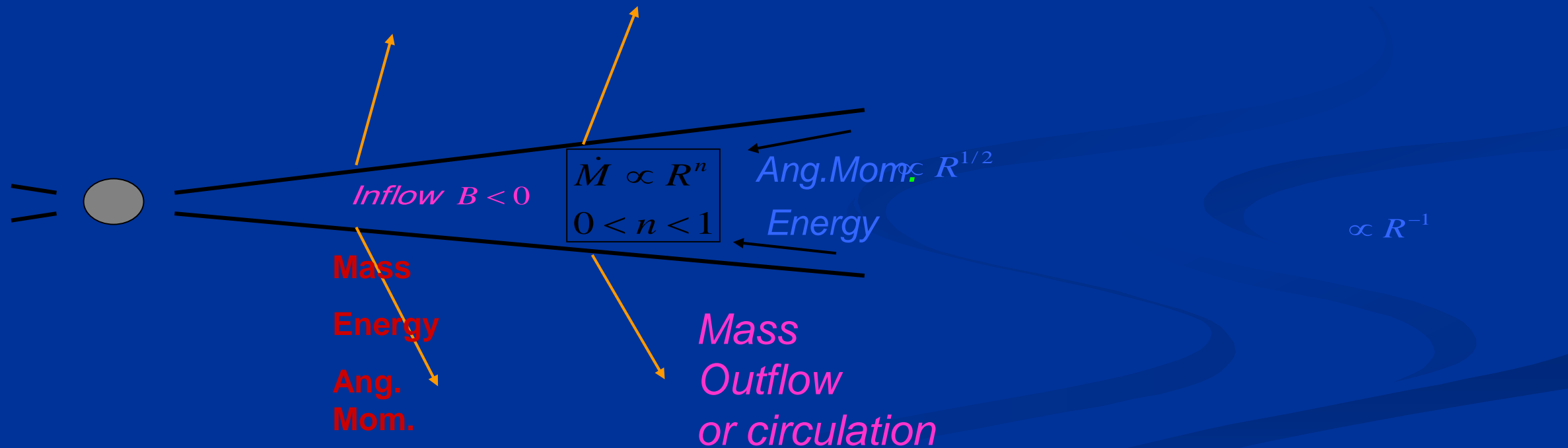
ACCRETION ONTO SUPERMASSIVE BLACK HOLES

❖ **Thick disk accretion:** Advection Dominated Inflow-Outflow Solution (ADIOS)

Blandford & Begelman (1999, 2004)

Most of gas is driven away \rightarrow only small amount accretes on the SMBH

\rightarrow SMBH grows slowly!



CONCLUSIONS FOR TALK 2

- ❖ Accretion disk physics is **fundamental** because it is basically the black hole physics
- ❖ AGN emerges as a **diverse class of objects** even when the central engine is only supermassive black holes
- ❖ We have **observational confirmation** that SMBHs reside in the AGN and power them in various ways
- ❖ The detailed physics of accretion flows is only now being understood as complicated, which has many solutions → **thin and thick disks, ADAFs, CDAFs, ADIOS, etc...**
- ❖ Still unsolved are many details, and especially that of what is the **source of fuel** which powers SMBHs