

# Geometry Factors pt. II, Error Analysis, and Optimizations

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Simulation Method

Error Analysis

Optimizations

# Simulation Goals

- Calculate geometry factors
- Optimize pressure and collimation variables
- Estimate running time

# Completed Improvements

- Using mersenne twistor generator
- Updated beam divergence model
- Change structure to weighted variables
- Addition of covariant errors
- Many small speedups
- Statistics anomaly resolved

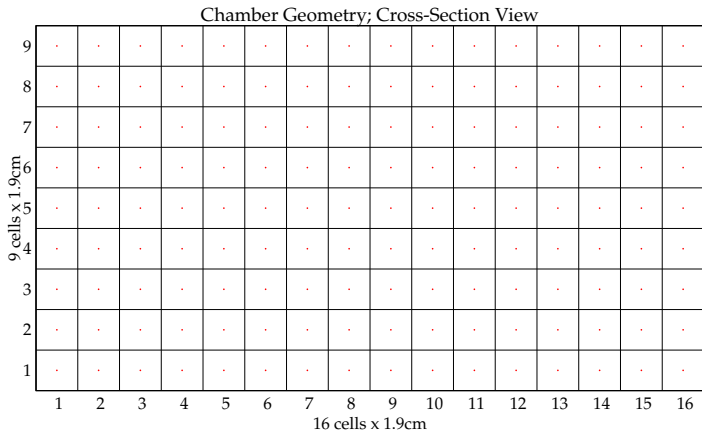
## Statistics-dependent effect

For simplicity, consider the diagonal approximation to the uncertainty:

$$\frac{1}{\sigma_d^2} \approx \sum_{\kappa} \frac{1}{\sigma_{\kappa}^2}$$
$$\sigma_d = \frac{1}{\sqrt{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_2^2} + \frac{1}{\sigma_3^2} + \dots}} = \frac{1}{\sqrt{\frac{G_1^2}{c_1} + \frac{G_2^2}{c_2} + \frac{G_3^2}{c_3} + \dots}}$$

The factors  $c_i$  consist of terms which converge very rapidly. The  $G_{\kappa}$  fluctuate randomly in  $(-1,1)$  as sample size is increased. As the sample size gets large, they approach their true value. Since they appear squared in all terms, factors which are slightly too large will have a significant effect on the value of  $\sigma_d$ . For statistically insufficient sample sizes,  $\sigma_d$  is underestimated. With a large enough sample size, the value stabilizes.

# Cell Diagram

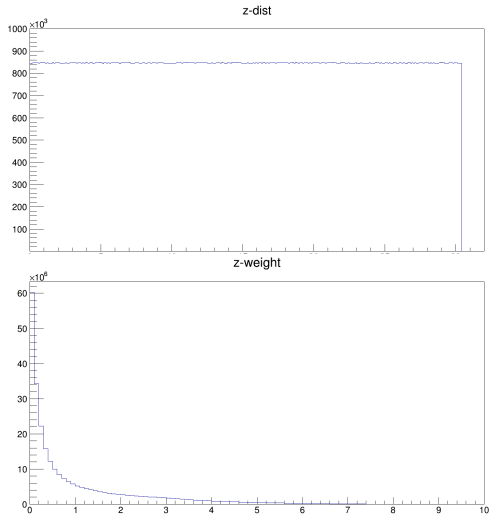


View in the yz-plane of the wire chamber.

# Cell Model

1. Model the wire chamber as 144 cells which collect all charge deposited in a parallelepiped set by the surrounding high voltage wires.
2. Each cell is 1.9 cm  $\times$  1.9cm  $\times$  17.1 cm. (There is a small correction to the volume of the top and bottom row of cells, since they are smaller).
3. Assume the  $^3\text{He}$  is contained inside the total cell volume. This is the  $^3\text{He}$  "buffer."

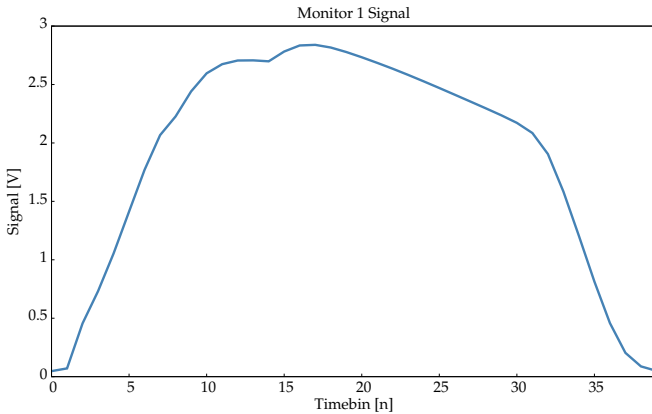
# Weighting Scheme



Instead of using kinematic variables, use normally distributed variables in  $x, y, z$ , and  $t$ , with corresponding weights.

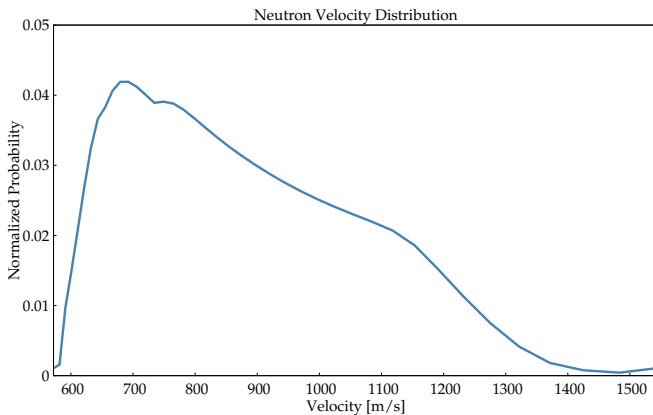


# Time Signal



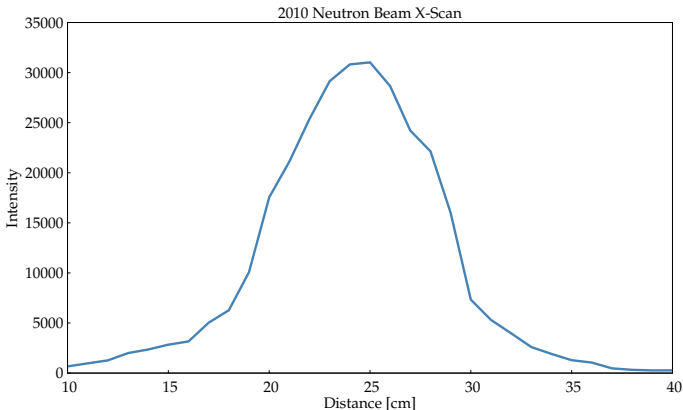
40-timebin neutron intensity signal from Monitor 1.

# Neutron Velocity Distribution



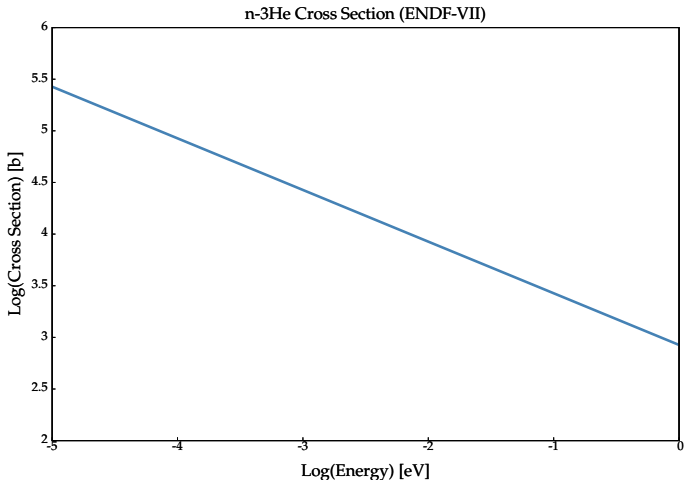
Velocity distribution generated from time-of-flight  
analysis:  $v = \frac{15.15}{.0098 + \frac{tbin}{2400}}$

# Beam Profile



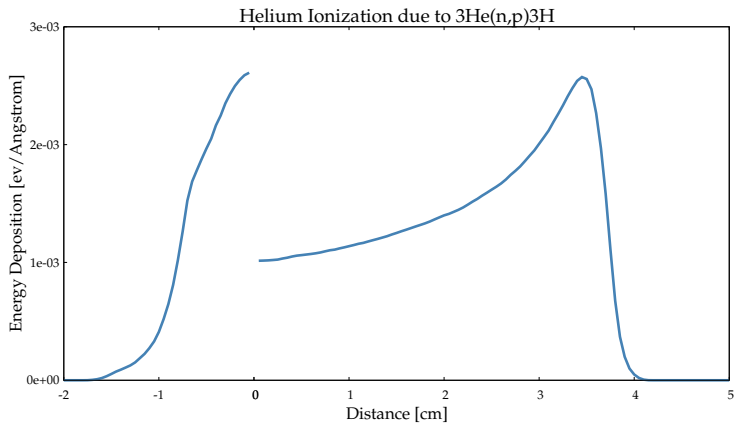
New fitting function for beam profiles based on gaussian dispersion model:  $I = \frac{I_0}{2} \left[ \text{Erf}\left(\frac{\mu-x}{\sigma\sqrt{2}}\right) + \text{Erf}\left(\frac{\mu+x}{\sigma\sqrt{2}}\right) \right]$

# Cross Section



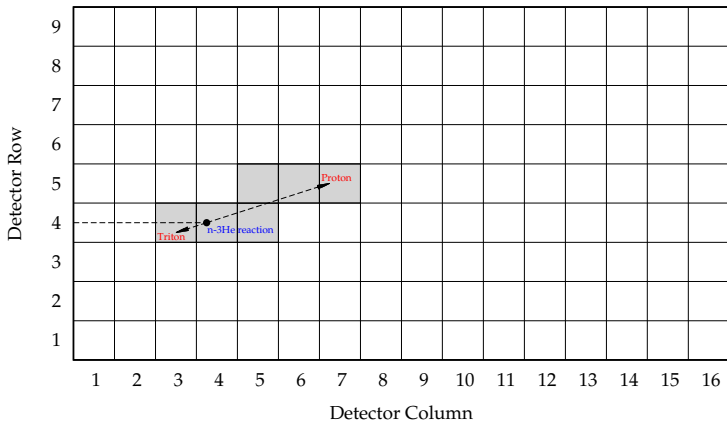
Cross section generated from function, rather than by lookup. Linear parameter found by fitting ENDF data to linear function:  $C = 2.92709$

# Ion Energy Deposition

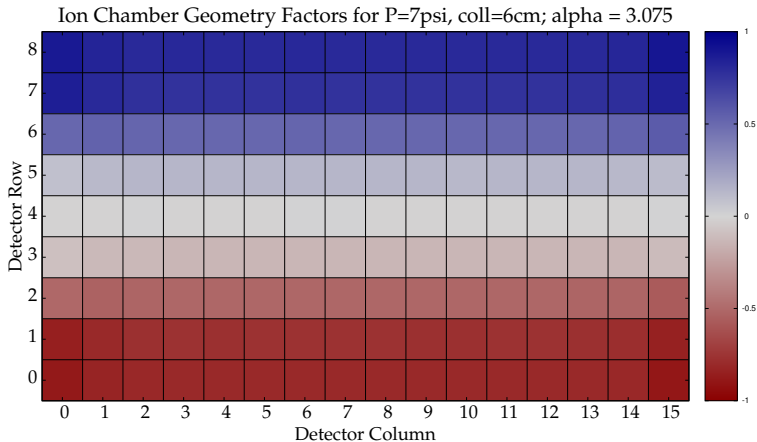


# Tracking Matrix

Example Reaction



# Geometry Factors



# Quantities

To calculate geometry factors and our dilution factor, we will need to track the mean energy deposited into a cell, the mean energy weighted by the cosine, and the mean covariant energy between two different cells.

$$\langle E^\kappa \rangle$$

$$\langle E^\kappa \cos \theta \rangle$$

$$\langle Q^{\kappa\beta} \rangle$$



## Calculation of $\alpha_\kappa$

The element asymmetry  $\alpha_\kappa$  depends on  $G_\kappa$  and the measured yields of that element.

$$Y_h^\kappa = \langle E^\kappa (1 + h\alpha \cos \theta) \rangle$$

$$\frac{Y_+^\kappa - Y_-^\kappa}{Y_+^\kappa + Y_-^\kappa} = \alpha_\kappa \frac{\langle E^\kappa \cos \theta \rangle}{\langle E^\kappa \rangle} \Rightarrow G_\kappa = \frac{\langle E^\kappa \cos \theta \rangle}{\langle E^\kappa \rangle}$$

$$\alpha_\kappa = \frac{1}{G_\kappa} \frac{Y_+^\kappa - Y_-^\kappa}{Y_+^\kappa + Y_-^\kappa}$$

## Calculation of $\alpha$

We will combine each element asymmetry to form the combined physics asymmetry.

$$\alpha = \sum_{\kappa} w_{\kappa} \alpha_{\kappa} = \vec{w} \cdot \vec{\alpha}$$

$$\sum_{\kappa} w_{\kappa} = 1$$

Choose weighting that minimizes uncertainty.

## Error in $\alpha$

$$\sigma_{\alpha}^2 = \sum_i \sum_j \frac{\partial \alpha}{\partial \alpha_i} \frac{\partial \alpha}{\partial \alpha_j} \sigma_{\alpha_i \alpha_j} = \sum_i \sum_j w_i w_j \sigma_{\alpha_i \alpha_j} = \vec{w}^T \cdot \hat{\sigma}_{ij} \cdot \vec{w}$$

Must have method to calculate  $\hat{\sigma}_{ij}$  from fundamental quantities:

$$\sigma_{\alpha_{\kappa} \alpha_{\beta}} = \frac{\langle Q^{\kappa \beta} \rangle}{2 \langle E^{\kappa} \cos \theta \rangle \langle E^{\beta} \cos \theta \rangle}$$

For diagonal elements, this reduces to:

$$\sigma_{\alpha_{\kappa}}^2 = \frac{\langle E^{\kappa^2} \rangle}{2 \langle E^{\kappa} \cos \theta \rangle^2}$$

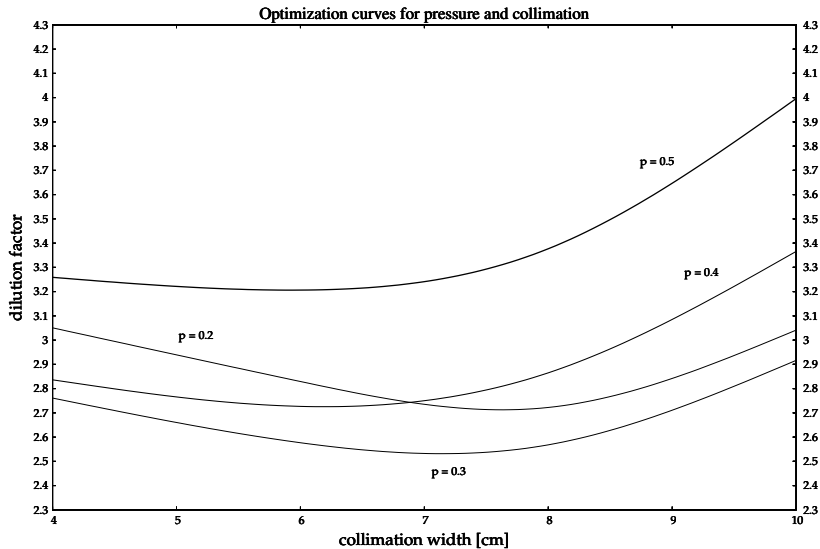
# Optimization

$$\frac{\partial \sigma_{\alpha_\kappa}^2}{\partial w_k} = \lambda_k \frac{\partial (\sum_i w_i - 1)}{\partial w_k}$$

$$\Rightarrow \text{minimized } \sigma_{\alpha_\kappa}^2 = \sum_i \sum_j \hat{\sigma}_{ij}^{-1}$$

Apply to pressure and collimation parameters.

# Results



# Planned Improvements

- New beam scan will improve precision of x-y positioning.
- Drift time analysis will give more realistic signal timing.

