

Geometric interpretation of the identity: $(\vec{a} \cdot \tilde{\vec{a}}) \vec{x} = \vec{a} (\tilde{\vec{a}} \cdot \vec{x}) - \tilde{\vec{a}} \times (\vec{a} \times \vec{x})$
 — nonorthogonal projection onto $\text{LINE} \oplus \text{PLANE}$ (direct sum)

$$\vec{x}_1 = \alpha \vec{a} \quad \text{where}$$

$$\alpha = \frac{x_1}{a} = \frac{x_{\parallel}}{a_{\parallel}} = \frac{\tilde{\vec{a}} \cdot \vec{x}}{\tilde{\vec{a}} \cdot \vec{a}}$$

$$\vec{x}_2 = -\tilde{\vec{a}} \times \vec{d} \quad \text{where}$$

$$d = \frac{x_2}{\tilde{a}} = \frac{x_{\perp}}{\tilde{a}_{\parallel}} = \frac{|\vec{a} \times \vec{x}|}{\vec{a} \cdot \tilde{\vec{a}}}$$

assuming
 $\vec{a} \cdot \tilde{\vec{a}} = 1$

