Section 4.3 - Electric Displacement D

* reviews: parallels between E and P

- ~ what are the units of $\varepsilon \bar{E}$? \bar{P} ?
- ~ both are vector fields (functions of position)
- ~ the field lines (flux) are associated with charge (Dr. Jekyll or Mr. Hyde ??)
- ~ the two fields are related: E induces P in a dielectric

Φ = Q V·ε, E=p ñ·Δε, E=σ total charge

 $\underbrace{P_{p} = Q_{b}}_{(+)} \nabla \cdot \vec{P} = P_{b} + \hat{n} \cdot \Delta \vec{P} = -\sigma_{b} + bound charge$ $\underline{\Phi_{p}} = Q_{f} + \nabla \cdot \vec{D} = P_{f} + \hat{n} \cdot \Delta \vec{D} = \sigma_{f} + free charge$ $\underline{D_{2}^{+} - D_{1}^{+} = \sigma_{f}} + \sigma_{f} + \sigma_{f} = \sigma_{f}$

* new field: D = "electric displacement"

~ defined by the "constitutive equation": $|\hat{D} = \varepsilon_0 \hat{E} + \hat{P}|$

~ associated with the free charge: lines of D flux go from (+) to (-) free charge

~ iterative cycle:

a) free charge generates E

(b) E causes P, diplaced bound charge (b) c) the field from bound charge modifies E

~ direct calculation procedure with D

- a) calculate D directly from free charge only
- b) obtain P from D using consititutive relation
- c) the electric field is: E = D-P

* differences between $\mathcal{E}_{o}\mathsf{E},\ \mathsf{P}$, and D :

- ~ equipotentials associated with force ==qE only for the electric field
- ~ p generates E, but P induces Ch

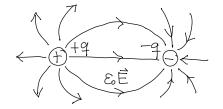
~ E=0 VXE=0 6xAE=0

 $\vec{E} = \int \frac{dq' \hat{x}}{4\pi \epsilon_0 x^2} \quad \vec{E} = \int \frac{dq' \hat{x}}{4\pi \epsilon_0 x^2} \quad \vec{E} = \int \frac{dq' \hat{x}}{4\pi \epsilon_0 x^2}$

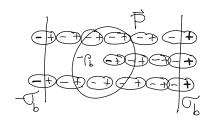
note: not P or D in these formulas!

* you need both $\nabla \cdot \vec{D} = p_f$ and $\nabla \times \vec{E} = 0$ to solve!

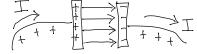
Electric field "E"



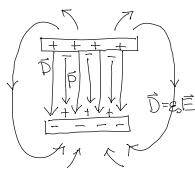
Polarization "P"



"Displacement current" (Maxwell) $\overline{J}_{d} = \frac{\partial \overline{D}}{\partial t}$



$$I_{d} = \int \vec{J}_{d} \cdot d\hat{a} = \int \frac{\partial \vec{D}}{\partial t} \cdot d\hat{a} = \frac{\partial \vec{\Phi}}{\partial t}$$



E-E-D-P inside $E_{A}E = D$ outside