L69-Zeeman effect

Monday, March 21, 2016

* review: structure of H-spectrum: dipole interactions. perturbative expansion on $\alpha = \frac{e^2}{4\pi \epsilon_0 hc} \sim 1/37$

Bohr levels -> En = -E/hr E°~ X2mc2 fine structure $\rightarrow E_n = \frac{-E_1^o}{n^2} \left(\frac{\lambda^2}{n^2} \left(\frac{n}{n^2} - \frac{34}{4} \right) \right)$ Es~ 24 MC2 ELS. ~ X5 MC2 Lambshift Elso 24 memc2

hyperfine struct. New quantum numbers: j, m; not just 1, 1 now! (total j,m;)

D.B interaction we with

· internal magnetic field proton orbit - fine structure prodon spin - hyperfine skuct.

· external magnetic field Zeeman effect (tunable)

P. P with external electric field Stark effect (also tuvable)

* in an external magnetic field, electron energy has an additional perturbation:

N/2 = - (M/Ms). Bext = 2m(L+23)· Bext = (gemet gsms) MBBext

 $\vec{\mu}_{e} = -g_{e} \cdot \frac{e\pi}{2m} \cdot \vec{L}_{h}$ $\vec{\mu}_{s} = -g_{s} \cdot \mu_{B} \cdot \vec{S}_{h}$ $g_{e} = 1$ Landé $\vec{\mu}_{s} = -g_{s} \cdot \mu_{B} \cdot \vec{S}_{h}$ $g_{s} = 2$ Suctors $\mu_{B} = 57.88 \, \mu eV/T$ Bohr magneton Y'= Ols · SIM

gyro magnetic ratio.

* perturbation theory depends on which "good" quantum numbers break the degeneracy of the Bohr energy levels.

a) if Bint >> Bext then j.m; good quantum numbers.

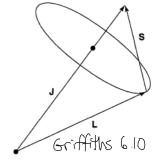
b) --- Bint & Bext -- m, ms ----

Bint = Bext must diagonalize complete perturbation.

Al wenk-field Feelmain effect:



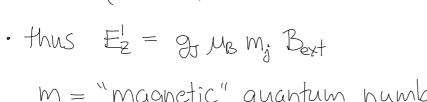
A) weak-field Zeeman effed: quantum #s: n,l,j,m; but not me, ms

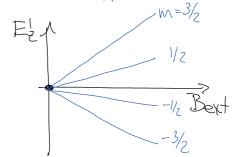


- · We must find the time-are of Me, Ms in H'z · I, S orbit around I, find their projection!

$$\langle \vec{L} + 2\vec{S} = \vec{J} + \vec{S} \rangle = \langle \vec{J} (1 + \vec{J} \cdot \vec{S}) \rangle = (1 + \frac{j(j+1) - g(l+1) + g(s+1)}{2 \cdot j(j+1)}) \vec{J}$$

where $(\vec{L} = \vec{J} - \vec{S})^2 = \vec{J}^2 + S^2 - 2\vec{J} \cdot \vec{S}$ 95 Landé Ructor





- m = "magnetic" quantum number. B-field breaks the m-degeneracy. B) Strong-field Zeeman effect $E_z' = \frac{92m}{B_{eff}} \cdot (\hat{L} + 2\hat{S})$ guantum $\frac{4}{S}$: n, l, m_e, m_s (H_z' breaks the degeneracy of n)
 - · Es is a pertur bothon to: Enlm, = -E1 + (me+2ms) MB Bext $\Xi'_{r} = \frac{[E_{N}]^{2} \left(\frac{4n}{1+1/2} - S\right)}{2mc^{2} \left(\frac{4n}{1+1/2} - S\right)}$ (sawe) $\pi'_{so} = \frac{e^{2}}{8\pi\epsilon} \frac{1}{m^{2}c^{2}r^{3}} \frac{S \cdot L}{\kappa^{2}m_{e}m_{s}}$
 - instead of $J^2 = (\tilde{L} + \tilde{S})^2 = L^2 + 2\tilde{L} \cdot \tilde{S} + S^2 \rightarrow L \cdot S = \frac{1}{2} (J^2 L^2 S^2)$ use (S.I) = (Sxlx+Syly+SzLz) = SzLz = tomems $E_{fs}^{1} = \frac{E_{1}^{1}}{N^{3}} \chi^{2} \left\{ \frac{3}{4n} - \frac{l(l+1) - m_{ems}}{l(l+1)\gamma(l+1)} \right\}$