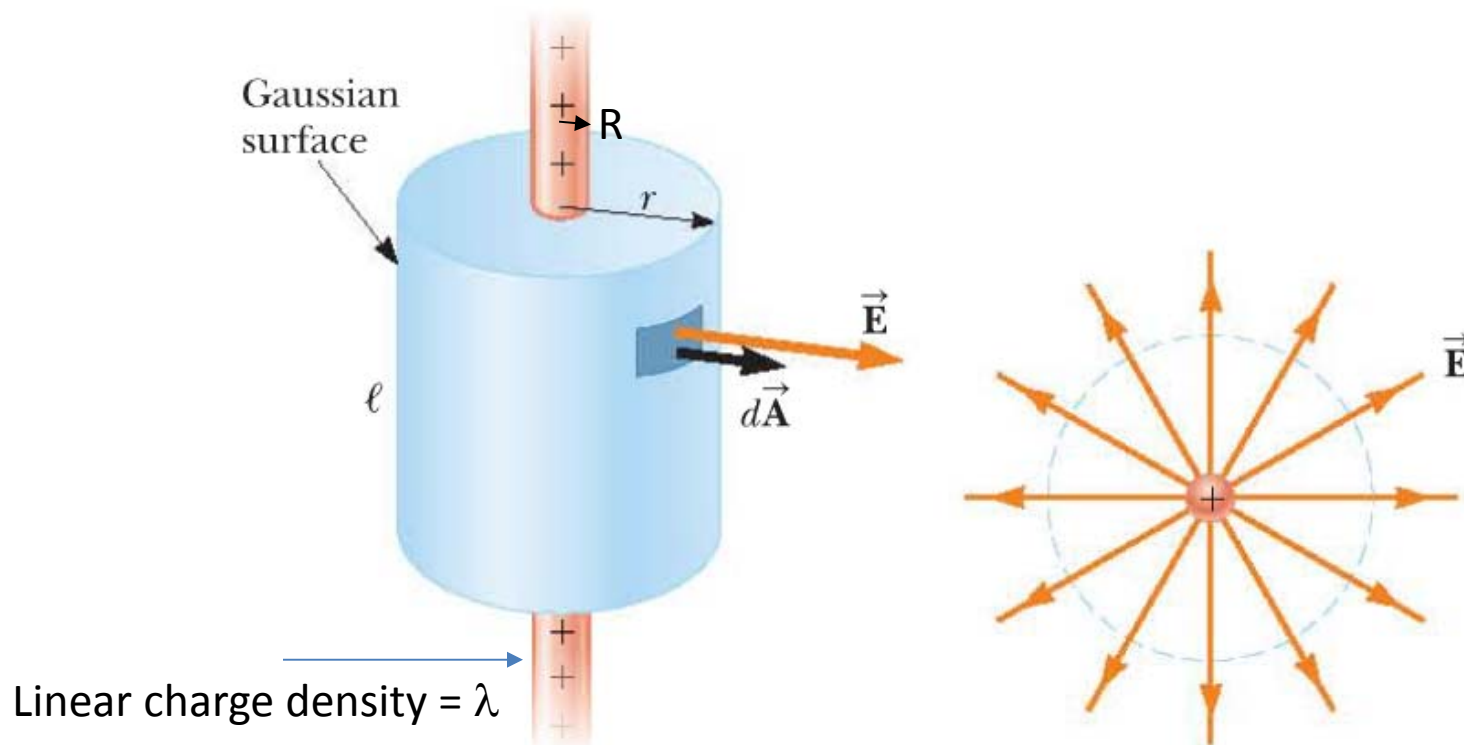


## Test Next Wednesday (Sept 20)

1. Chapter 5 and 6.
2. 45 minutes sharp.
3. 4 multiple choices and 2 long problems.
4. Formula sheet provided.
5. Contact me before next Monday for prearrangement if you need special accommodation.

## Application of Gauss's Law II

# Uniform cylindrical (infinite long) distribution



$$\text{For } r > R \quad \epsilon_0 \Phi_E = q_{\text{in}} \Rightarrow \epsilon_0 \cdot E \cdot 2\pi r \ell = \lambda \ell$$

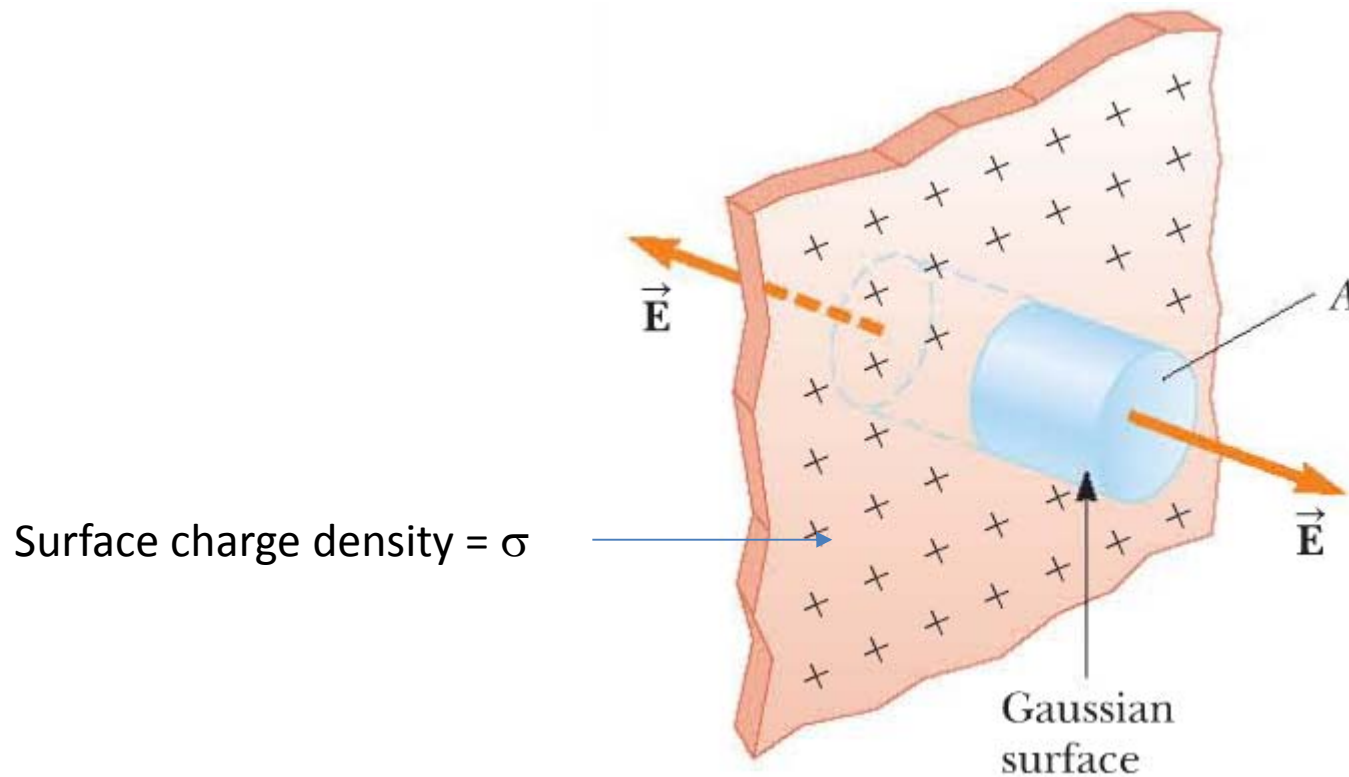
$$\Rightarrow E = \frac{\lambda}{2\pi\epsilon_0 r}$$

Note that a line point charge belongs to this case.

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For  $r < R$  Depends on the actual charge distribution.

# Uniform distribution in an infinite plane



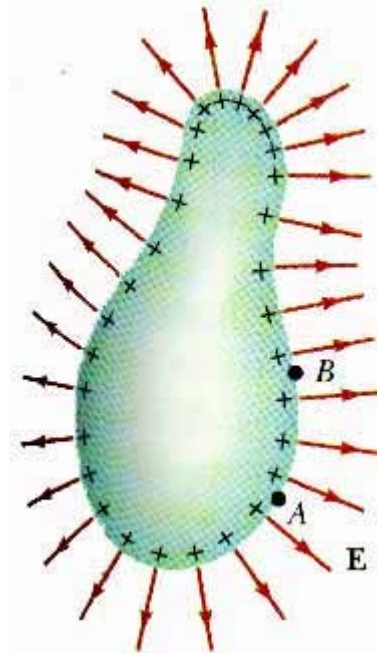
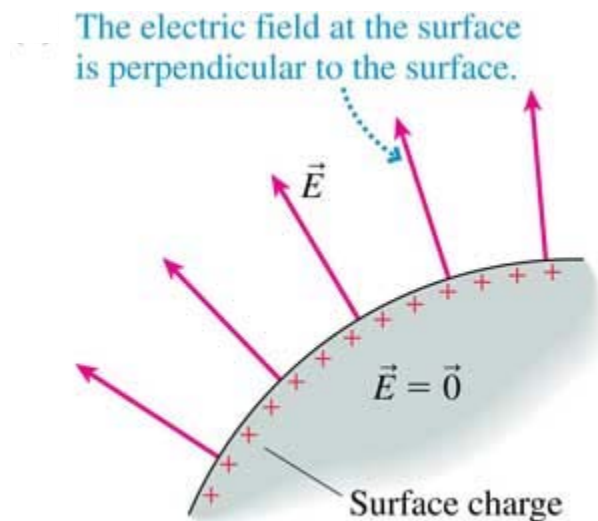
$$\epsilon_0 \Phi_E = q_{\text{in}} \Rightarrow \epsilon_0 \cdot 2 \cdot E \cdot A = \sigma A$$

$$\Rightarrow E = \frac{\sigma}{2 \epsilon_0} \quad \text{Note field is constant}$$

## More on Conductors

The following are true for any shape of a conductor, including the ones with cavities inside it (but assume there is no charge inside the cavities).

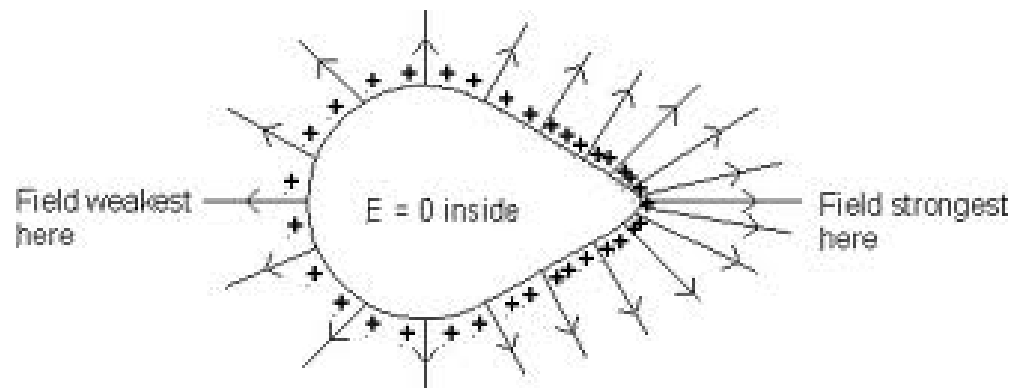
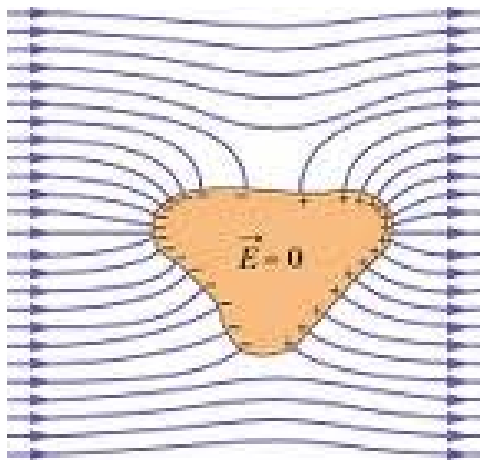
- 1.If the conductor has a net charge, all charges will stay only on the surfaces of the conductor.
- 2.There is no electric field inside the conductor.
- 3.The electric field outside the outer surface always perpendicular to the surface in the proximity of the conductor.



# All on Conductors (as a Source of Electric Field)

(Con't)

4. Electric field is stronger at the sharper part (smaller radius of curvature) of the outer surface.



(d) Electric field & charge distribution around a pear-shaped conductor

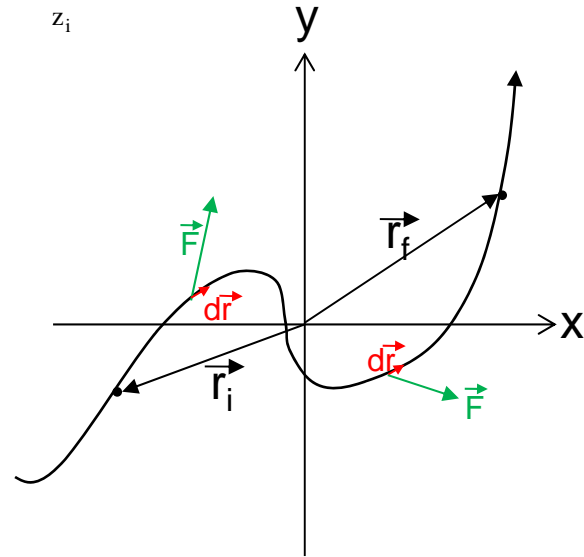
# Class 11. Electric Potential Energy and Electric Potential

# Work

Work done  $W$  by a force  $\vec{F} = \int_{x_i}^{x_f} F_x dx + \int_{y_i}^{y_f} F_y dy + \int_{z_i}^{z_f} F_z dz$

$$\begin{aligned}\vec{F} &= \int_{x_i}^{x_f} F_x dx + \int_{y_i}^{y_f} F_y dy + \int_{z_i}^{z_f} F_z dz \\ &= \int_{x_i}^{x_f} F_x dr_x + \int_{y_i}^{y_f} F_y dr_y + \int_{z_i}^{z_f} F_z dr_z\end{aligned}$$

Work done  $W$  by a force  $\vec{F} = \int_{\vec{r}_i}^{\vec{r}_f} \vec{F} \cdot d\vec{r}$





# Potential energy

$$\Delta K = K_f - K_i = \text{Work done by electric force } \vec{F}_E \\ + \text{Work done by other forces } \vec{F}_i$$

Static electric is conservative, so we can define electric potential energy  $U_E$  as :

$$\Delta U_E = - \text{Work done by electric force } \vec{F}_E$$

$$\therefore \Delta K = -\Delta U_E + \text{Work done by other forces } \vec{F}_i$$

$$\Rightarrow \Delta K + \Delta U = \text{Work done by other forces } \vec{F}_i$$

