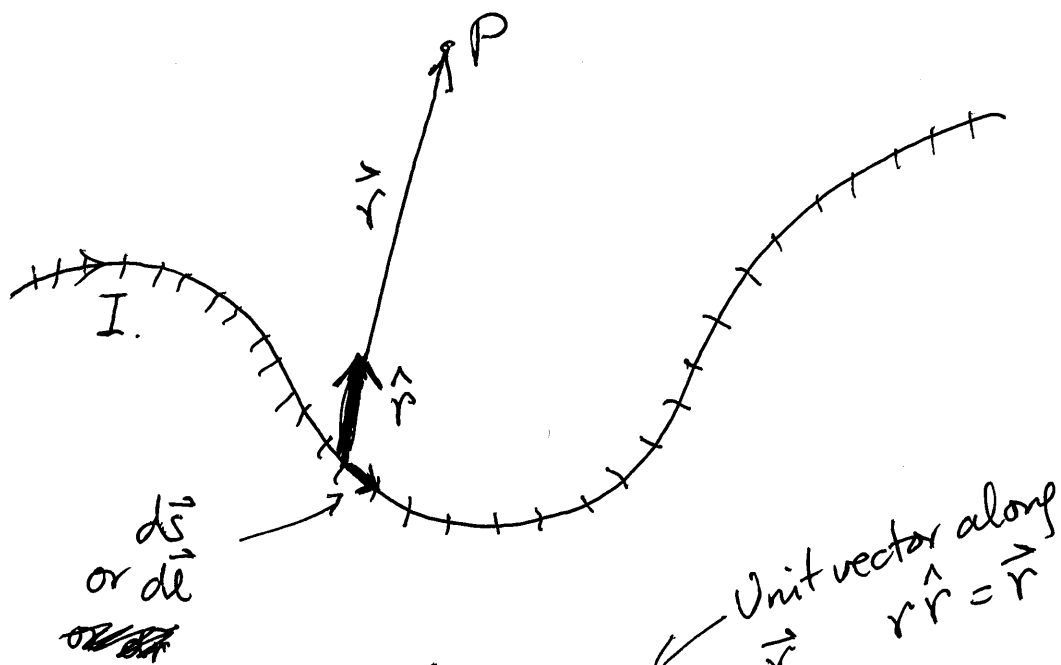


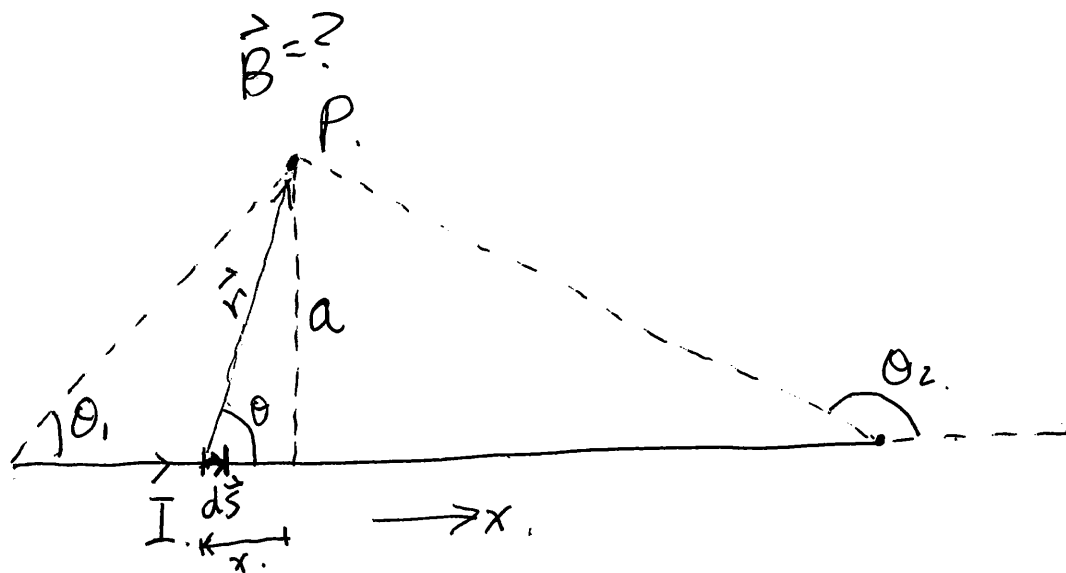


$$d\vec{B} = \frac{\mu_0}{4\pi} \left(\frac{I d\vec{s} \times \hat{r}}{r^2} \right)$$

a very small vector

magnitude of $\vec{r}$

Unit vector along $\vec{r}$. $r\hat{r} = \vec{r}$



$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{s} \times \hat{r}}{r^2}$$

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{dx \sin \theta}{r^2} \quad (1)$$

$$\tan \theta = \frac{a}{x} \Rightarrow x = \frac{a}{\tan \theta} = -a \cot \theta.$$

$$dx = + \frac{a d\theta}{\sin^2 \theta}.$$

$$a = r \sin \theta \Rightarrow r = \frac{a}{\sin \theta}.$$

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \cdot \frac{+ \frac{a d\theta}{\sin^2 \theta}}{\left(\frac{a}{\sin \theta}\right)^2} \sin \theta \quad (1)$$

$$= + \frac{\mu_0 I}{4\pi a} \sin \theta d\theta \odot$$

$$\vec{B} = + \frac{\mu_0 I}{4\pi a} \odot \int_{\theta_1}^{\theta_2} \sin \theta d\theta$$

$$= - \frac{\mu_0 I}{4\pi a} \odot [\cos \theta]_{\theta_1}^{\theta_2}$$

$$= - \frac{\mu_0 I}{4\pi a} \odot (\cos \theta_2 - \cos \theta_1)$$

$$= \frac{\mu_0 I}{4\pi a} (\cos \theta_1 - \cos \theta_2) \odot$$

For infinite long wire,

$$\theta_1 = 0^\circ, \quad \theta_2 = 180^\circ$$

$$\vec{B} = \frac{\mu_0 I}{4\pi a} (1 - (-1)) \odot = \frac{\mu_0 I}{2\pi a} \odot$$