

Consider the example in Problem 8. Calculate A so that $\psi(x)$ is probably normalized.

[Problem 2-8:

Consider a wave function of the form

$$\psi(x) = Ae^{-\mu|x|}$$

Calculate the wave function in momentum space $\phi(p)$.]

Solution: $\psi(x) = Ae^{-\mu|x|}$

$$\int_{-\infty}^{\infty} \psi^*(x)\psi(x)dx = 1 \Rightarrow \int_{-\infty}^{\infty} (Ae^{-\mu|x|})^2 dx = 1$$

$$\Rightarrow \int_{-\infty}^{\infty} A^2 e^{-2\mu|x|} dx = 1$$

$$\Rightarrow A^2 \left(\int_{-\infty}^0 e^{2\mu x} dx + \int_0^{\infty} e^{-2\mu x} dx \right) = 1$$

$$\Rightarrow A^2 \left(\frac{1}{2\mu} [e^{2\mu x}]_{-\infty}^0 + \frac{1}{-2\mu} [e^{-2\mu x}]_0^{\infty} \right) = 1$$

$$\Rightarrow A^2 \left[\frac{1}{2\mu} + \left(-\frac{1}{-2\mu} \right) \right] = 1$$

$$\Rightarrow A^2 \left[\frac{1}{\mu} \right] = 1$$

$$\Rightarrow A^2 = \mu$$

$$\Rightarrow A = \underline{\underline{\sqrt{\mu}}}$$