PHY 232 Summer 2016 Class Work Class 14. Parallel plate capacitor

Given ϵ_0 =8.8542×10⁻¹² C²m⁻²N⁻¹ and e= 1.6022×10⁻¹⁹ C.

A capacitor is formed by putting two square plates each of $4m^2$ in area parallel to each other with a separation of 1mm. The two plates are kept at a potential difference of 12V.

(a) Calculate the capacitance of this parallel plate capacitor.

$$C = \frac{\varepsilon_0 A}{d} = \frac{8.854 \times 10^{-12} \times 4}{0.001} = \frac{3.542 \times 10^{-8} \text{ F, or } 35.42 \text{nF}}{1.000 \times 10^{-8} \text{ F, or } 35.42 \text{nF}}$$

(b) What is the charge in one of the plate?

$$C = \frac{Q}{V} \implies Q = CV \implies Q = 3.542 \times 10^{-8} \times 12 = \underbrace{4.250 \times 10^{-7} \text{ C, or } 0.425 \,\mu\text{C}}_{=0.005}$$

(c) What is the electric field inside the gap between the plates?

$$V = Ed \implies E = \frac{V}{d} \implies E = \frac{12}{0.001} = \underbrace{1.2 \times 10^4 \text{ V, or } 12 \text{ kV}}_{}$$

(d) What is the energy stored in the capacitor?

(e) What is the energy density?

$$u_{\rm E} = \frac{1}{2} \varepsilon_0 E^2 = \frac{1}{2} \times 8.854 \times 10^{-12} \times (1.2 \times 10^4)^2 = \underline{6.375 \times 10^{-4} \text{ J/m}^3}$$