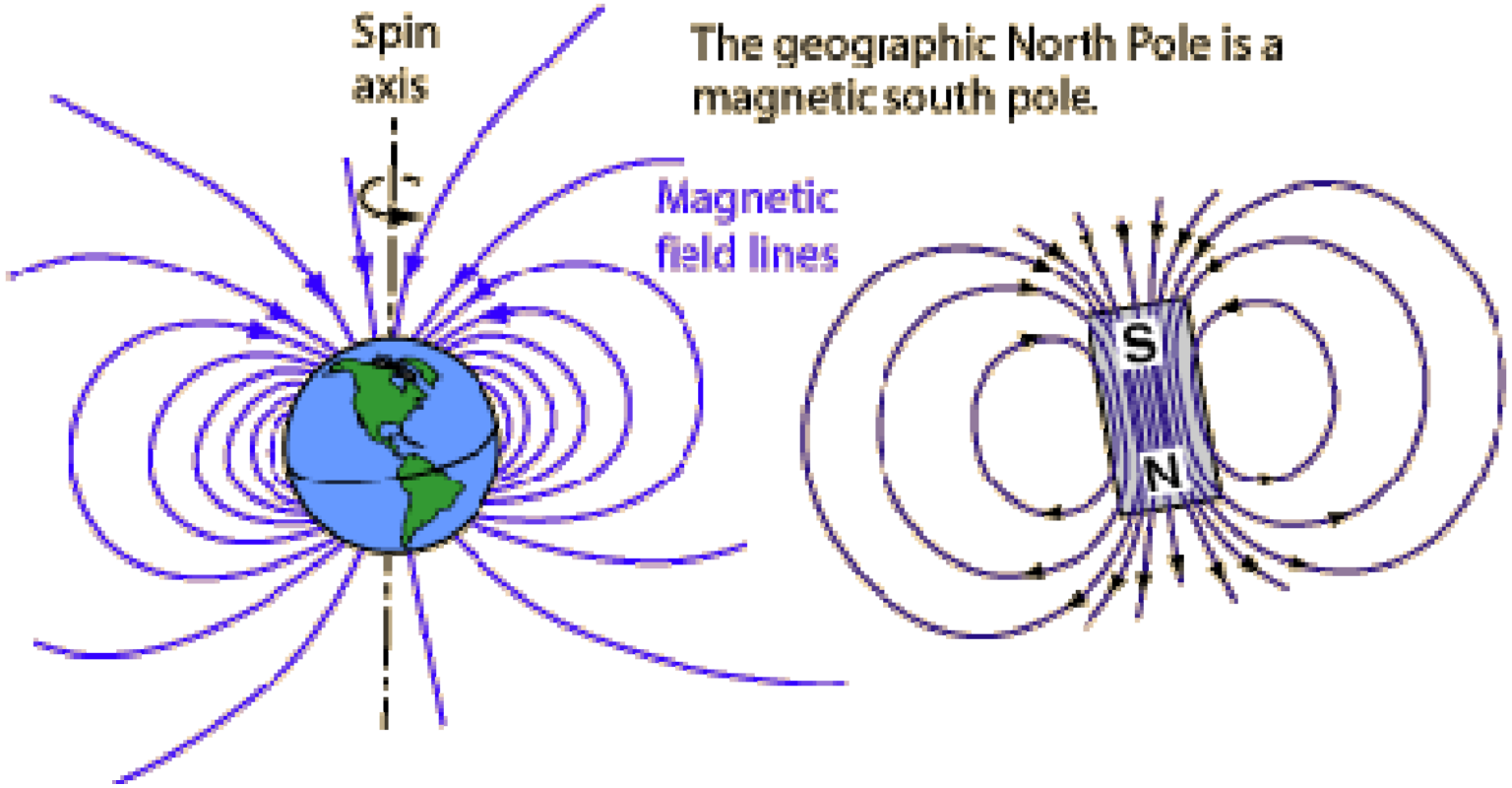
Class 23 Magnetic Force on a Moving Charge

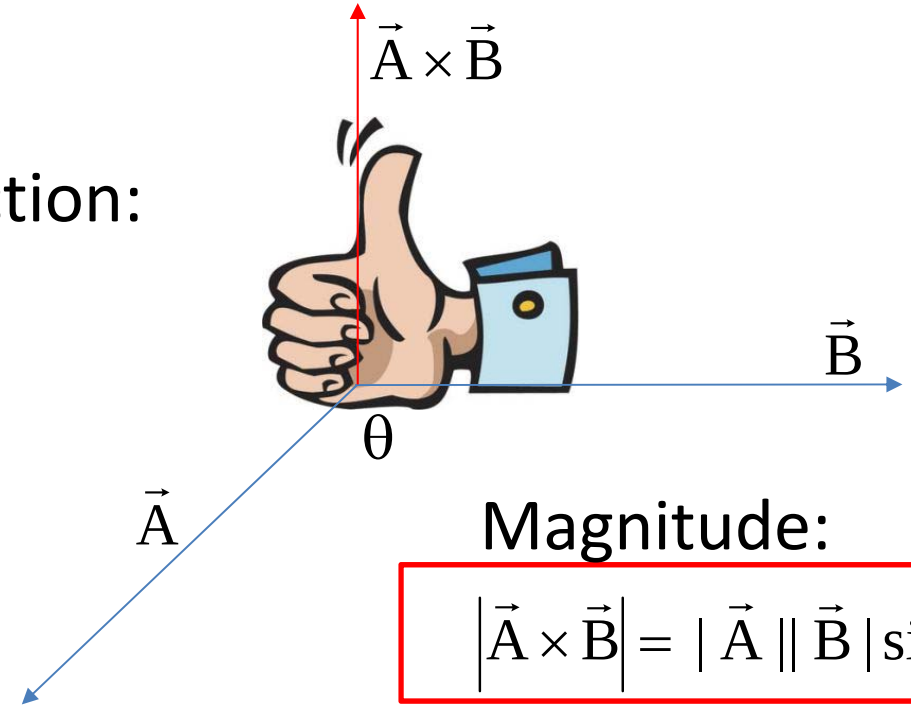
Magnetic Field



1. All single magnets have two poles, N and S.
2. Externally, magnetic field lines come out from the N pole and getting into the S pole.
3. Between two magnets, like poles repel and unlike poles attract.
4. The geographical north pole of earth is actually the S pole of a bar magnet.
5. We will explain why there is magnetic field later.

cross product between two vectors

Direction:



Magnitude:

$$\left|\vec{A} \times \vec{B}\right| = |\vec{A}||\vec{B}|\sin\theta$$

$$\vec{A} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ A_x & A_y & A_z \\ B_x & B_y & B_z \end{vmatrix} = \hat{i}\begin{vmatrix} A_y & A_z \\ B_y & B_z \end{vmatrix} - \hat{j}\begin{vmatrix} A_x & A_z \\ B_x & B_z \end{vmatrix} + \hat{k}\begin{vmatrix} A_x & A_y \\ B_x & B_y \end{vmatrix}$$

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$$

From class 3

A common symbol

or

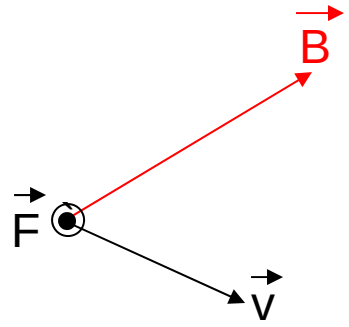
A vector perpendicular and pointing into the screen /paper.

or

A vector perpendicular and pointing out of the screen /paper.

Magnetic Force Acting on a Moving Charge

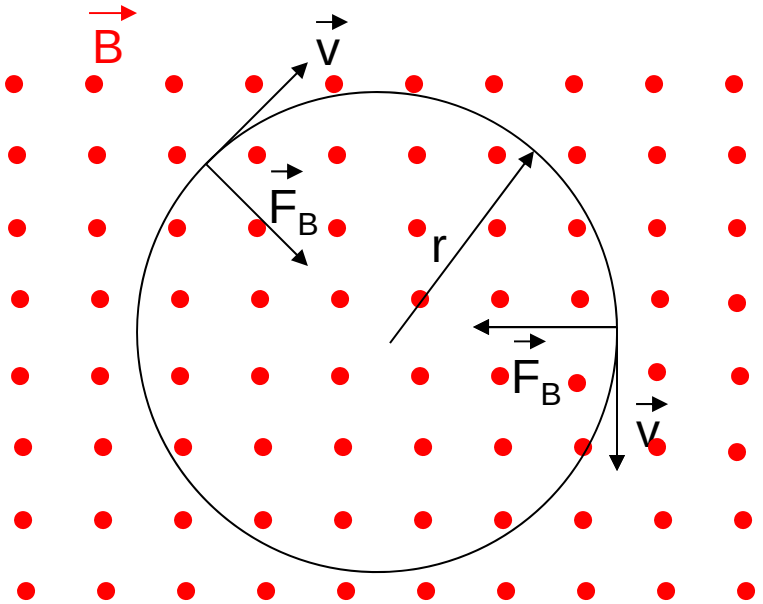
When a charge particle moves in a magnetic field B, there will be magnetic force acting on the particle:



$$\vec{F}_B = q\,\vec{v} \times \vec{B}$$

1. Unit of magnetic field is Tesla (T).
2. If there is magnetic field, only under two conditions the magnetic force on the charge particle will be zero: (i) the particle is not moving (v=0), or (ii) it is moving in parallel or antiparallel to the magnetic field ($\sin\theta=0$).
3. The magnetic force is always perpendicular to the magnetic field and the velocity.
4. The magnetic force does no work because $\vec{F}_B \cdot \vec{v} = 0$.
5. If you want to determine the direction acting on a negative charge particle, treat it like a positive charge first, then reverse the force direction at the end.

Motion of Charge Particle in a Uniform B field
$\Rightarrow$ Circular Motion of Constant Speed



1. $\vec{F}_B$ always perpendicular to $\vec{v} \Rightarrow$ Centripetal force
2. Magnetic force does no work $\Rightarrow$ Constant speed

Equation of motion:

$$q|v \times B| = m\frac{v^2}{r} \Rightarrow \boxed{qvB = m\frac{v^2}{r}} \Rightarrow \frac{v}{r} = \frac{q}{m}B$$

$$\Rightarrow \omega = \frac{q}{m}B \leftarrow \text{Cyclotgron frequency}$$