

Faraday's Law

changing
B.

changing
A.

Will Cause E
(New).

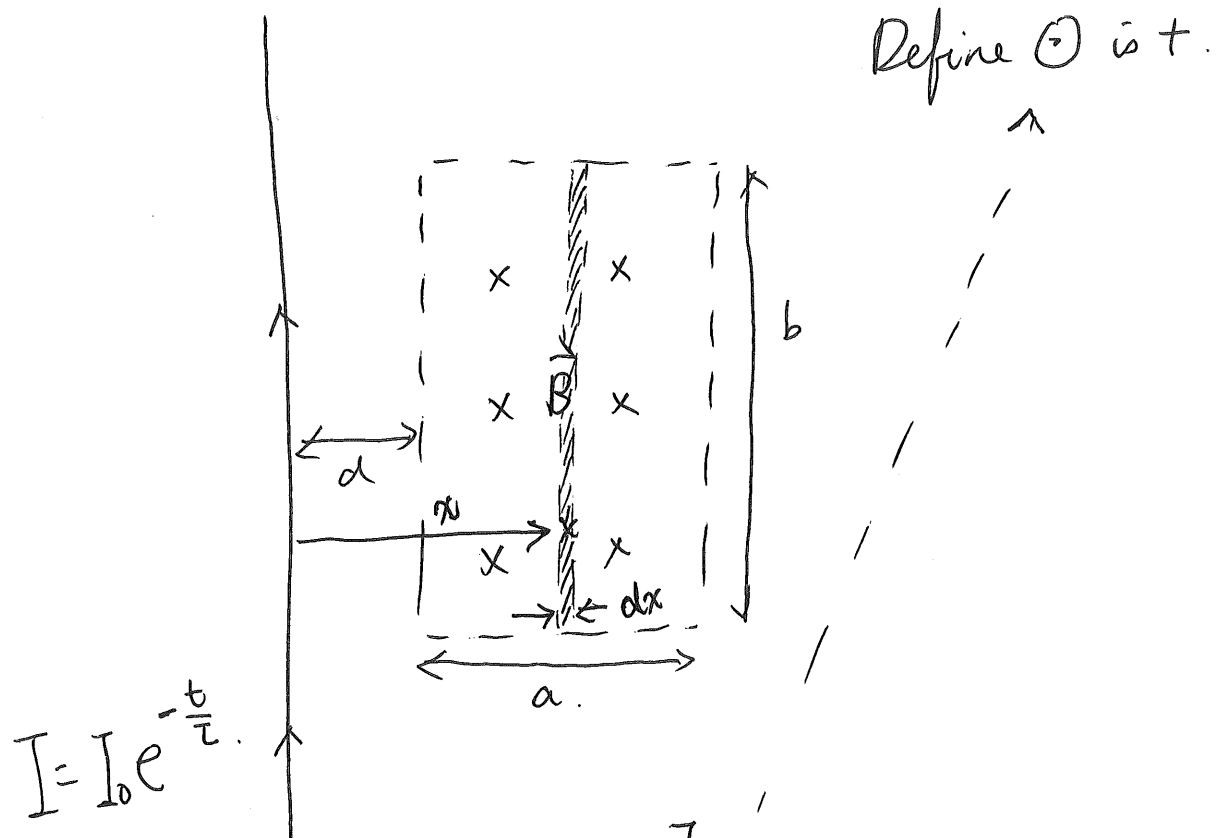
$$\mathcal{E} = -\frac{d}{dt} \Phi_B$$

$$\vec{F} = q\vec{v} \times \vec{B}$$

or $I\vec{L} \times \vec{B}$.

(only if you have
charges).

Maxwell's
4th Eq.



$$B = \frac{\mu_0 I}{2\pi x} \otimes$$

Flux of the infinitesimal element

$$= \frac{\mu_0 I}{2\pi x} \cdot b dx$$

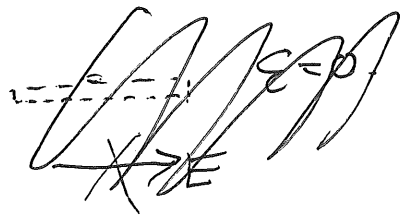
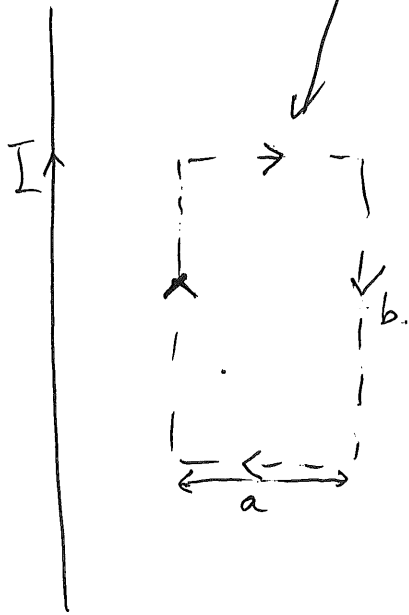
$$\Phi = - \int_a^{a+b} \frac{\mu_0 I}{2\pi x} b dx.$$

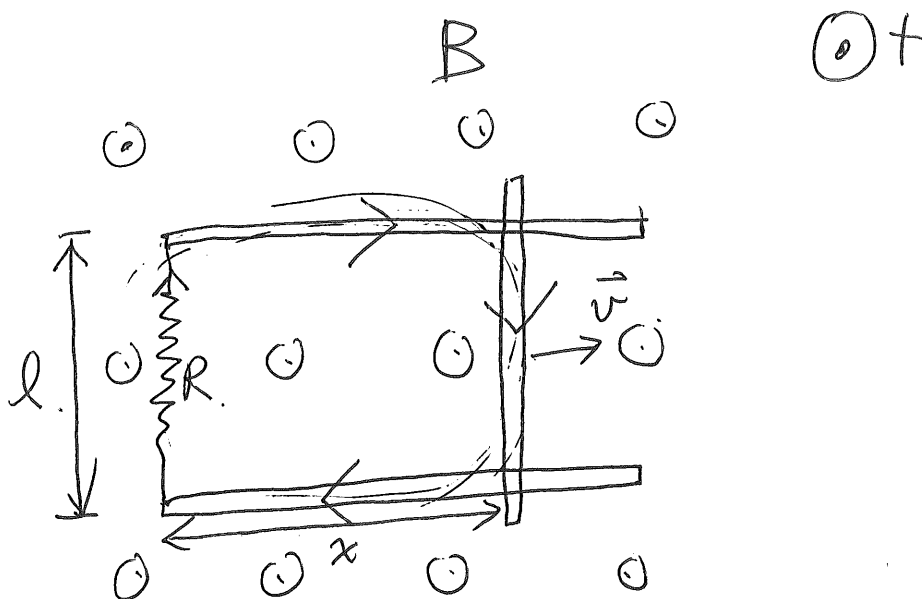
$$= - \frac{\mu_0 I b}{2\pi} \left[\ln x \right]_a^{a+b} = - \frac{\mu_0 I b}{2\pi} \ln \frac{a+b}{a}$$

$$I = I_0 e^{-t/\tau} \quad (I_0, \tau \text{ are constant}).$$

$$\Phi = \left(\frac{\mu_0 b}{2\pi} \ln \frac{d+a}{a} \right) I_0 e^{-\frac{t}{\tau}}.$$

$$\begin{aligned} \text{Emf: } \oint \vec{E} \cdot d\vec{s} &= - \frac{d\Phi}{dt} \\ &= - \frac{d}{dt} \left[- \left(\frac{\mu_0 b}{2\pi} \ln \frac{d+a}{a} \right) I_0 e^{-\frac{t}{\tau}} \right] \\ &= \frac{\mu_0 b}{2\pi\tau} \left(\ln \frac{d+a}{a} \right) I_0 e^{-\frac{t}{\tau}}. \end{aligned}$$





$$\text{Flux } \Phi = BA = Blx.$$

$$\mathcal{E} = -\frac{d\Phi}{dt} = -Bl \frac{dx}{dt}$$

$$= -Blv. \quad \checkmark$$

$\nwarrow$

Faraday's Law.

Ohm's Law

$$I = \frac{\mathcal{E}}{R} = -\frac{Blv}{R}.$$